

# **GENERAL INFORMATION**

| Course information  |   |  |  |  |  |  |  |
|---------------------|---|--|--|--|--|--|--|
| Name                | Stochastic optimization   |  |  |  |  |  |  |
| Code                | MRE-524   |  |  |  |  |  |  |
| Degree              | Master's Degree in Research in Engineering Systems Modeling (MRE) |  |  |  |  |  |  |
| Year                | 1 <sup>st</sup>   |  |  |  |  |  |  |
| Semester            | 2 <sup>nd</sup> (Spring) (even year)                              |  |  |  |  |  |  |
| <b>ECTS</b> credits | 3   |  |  |  |  |  |  |
| Type                | Elective  |  |  |  |  |  |  |
| Department          | Industrial Organization   |  |  |  |  |  |  |
| Area                | Statistics and Operations Research                                |  |  |  |  |  |  |
| Coordinator         | Andrés Ramos  |  |  |  |  |  |  |

| Instructor   |                                    |  |  |  |  |  |  |
|--------------|------------------------------------|--|--|--|--|--|--|
| Name         | Andrés Ramos                       |  |  |  |  |  |  |
| Department   | Industrial Organization            |  |  |  |  |  |  |
| Area         | Statistics and Operations Research |  |  |  |  |  |  |
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| Office hours | Arrange an appointment by email    |  |  |  |  |  |  |



#### **DETAILED INFORMATION**

#### Contextualization of the course

## Contribution to the professional profile of the degree

This subject introduces the student in simulation and data analysis techniques for supporting decision-making.

Specifically, the contributions of this course to the professional profile are the following:

- Knowing the application of system simulation in real environments, pros and cons of their use.
- Designing and developing stochastic optimization models using a simulation language
- Developing a practical work applied to support decisions in a realistic case study

This subject has both theoretical and practical components, based on the exposition and discussion of each topic but also on the application of the simulation and data analysis techniques to realistic case studies.

## **Prerequisites**

Students willing to take this course should be familiar with linear algebra, and undergraduate-level programming. Previous experience with any modeling language is also desired although not strictly required.



## **CONTENTS**

## **Contents**

#### **Theory**

## **Chapter 1. Introduction**

- 1.1 Generation expansion planning case study. Manufacturing case study.
- 1.2 Decision tree and scenario tree.
- 1.3 Two-stage and multistage linear optimization. Hydrothermal coordination problem case study

## **Chapter 2. Linear optimization**

- 2.1. Simplex method.
- 2.2. Duality.

## Chapter 3. Decomposition techniques

- 3.1 Fixed cost transportation problem.
- 3.2 Benders decomposition. Nested Benders decomposition.
- 3.3 Dantzig-Wolfe decomposition. Lagrangian relaxation.
- 3.4 Additional improvement in decomposition techniques.
- 3.5 Stochastic dual dynamic programming.

## Chapter 4. Scenario tree

- 4.1 Characterization
- 4.2 Generation



## Competences and Learning Outcomes

#### Competences

## **General Competences**

#### **Basic Competences**

CB2. To know how to apply and integrate knowledge, the understanding of it, its scientific basis, and problem-solving capabilities in new and loosely defined environments, including multidisciplinary contexts, both for research and highly-specialized professions.

#### **Specific Competences**

CE9. To know techniques, methods and/or necessary tools to carry out a specific research topic in a sector or particular technological context.

## **Optional Competences**

- CO3. To understand the statistical concepts associated to the representation of random parameters.
- CO4. To understand the mathematical principles of linear optimization, sensibility analysis and duality and the ability to use them.

#### Learning outcomes

At the end of the course the student must have the following competences:

- RA1. Understand the concepts of stochastic optimization
- RA2. Become familiar within the several topics where stochastic optimization can be applied
- RA3. Know how to build an optimization model efficiently
- RA4. Achieve mathematical rigorousness
- RA5. Understand the mathematical techniques used
- RA6. State and solve mockup problems
- RA7. Analyze the solutions
- RA8. Be prepared to extend their knowledge
- RA9. Become familiar with an algebraic language used professionally



# **TEACHING METHODOLOGY**

## General methodological aspects

The objective is improving the learning and incentivizing the autonomous and critical thinking of the students. For that purpose the following teaching resources are used.

The teaching resources mentioned require the active participation of the student. It is indispensable that the class activity would be complemented with the personal work of the student and, coherently, it will be taken into account to assess the student performance.

| <u>'</u>   |               |  |  |  |  |  |  |
|--|---------------|--|--|--|--|--|--|
| In-class activities  | Competences   |  |  |  |  |  |  |
| <ul> <li>Master lectures (20h): presentation of the contents of the subject.</li> </ul>  | CB1, CB2, CE2 |  |  |  |  |  |  |
| <ul> <li>Public presentation of the assignments (10h)</li> </ul>   | CE3           |  |  |  |  |  |  |
| Out-of-class activities  | Competences   |  |  |  |  |  |  |
| Personal work of the student (30h): study of the contents provided in the<br>master lectures. It requires a deep and critical analysis about modeling<br>aspects of the optimization problems allowing different perspectives and<br>incentivizing creativity and critical thought of the student. | CB1, CE2      |  |  |  |  |  |  |
| Assignments (30h): improve knowledge of the techniques presented.  | CB2, CE3      |  |  |  |  |  |  |



# ASSESSMENT AND GRADING CRITERIA

| Assessment activities   | Grading criteria  | Weight |
|-------------------------|---|--------|
| Case study              | <ul> <li>Practical case statement</li> <li>Model development</li> <li>Theoretical contribution</li> <li>Solution analysis</li> <li>Written communication skill</li> <li>Teamwork (if done in a team)</li> </ul> | 80%    |
| Communication skill     | Oral presentation of the case study   | 15%    |
| Classroom participation | Attendance and active participation in class  | 5%     |

# **GRADING AND COURSE RULES**

## Grading

#### Regular assessment

Case study will account for the 100%, of which:

Written report: 80%Oral presentation: 15%Participation: 5%

In case that the *written report mark* is equal or lower than 3.5, the final grade will be the *written report mark*. Otherwise, the final grade is computed weighting the different marks as the previously shown percentages. In order to pass the course, the final grade should be greater or equal to 5.0.

#### **Retakes**

The final grade is computed based only in a new written report about the same or different case study. In order to pass the course, the final grade should be greater or equal to 5.0.

#### Course rules

- Class attendance is mandatory according to Article 93 of the General Regulations (Reglamento General) of Comillas Pontifical University and Article 6 of the Academic Rules (Normas Académicas) of the ICAI School of Engineering. Not complying with this requirement may have the following consequences:
  - Students who fail to attend more than 15% of the lectures may be denied the right to take the final exam during the regular assessment period.

Students who commit an irregularity in any graded activity will receive a mark of zero in the activity and disciplinary procedure will follow (cf. Article 168 of the General Regulations (Reglamento General) of Comillas Pontifical University).

# WORK PLAN AND SCHEDULE<sup>1</sup>

<sup>&</sup>lt;sup>1</sup> A detailed work plan of the subject can be found in the course summary sheet (see following page). Nevertheless, this schedule is tentative and may vary to accommodate the pace of the class.



| In and out-of-class activities                                | Date/Periodicity   | Deadline |
|---|--|----------|
| Case study sessions   | Every week   |          |
| Review and self-study of the concepts covered in the lectures | After each lesson  |          |
| Problem-solving   | Weekly   |          |
| Case study report writing                                     | December   |          |
| Case study oral presentation                                  | During the course<br>and, in particular,<br>the last part of the<br>course |          |

| STUDENT WORK-TIME SUMMARY  |            |    |    |  |  |  |  |  |
|--|------------|----|----|--|--|--|--|--|
| IN-CLASS HOURS   |            |    |    |  |  |  |  |  |
| Lectures Problem-solving Case sessions Practices                 |            |    |    |  |  |  |  |  |
| 15   | 5          | 5  | 5  |  |  |  |  |  |
| OUT-OF-CLASS HOURS   |            |    |    |  |  |  |  |  |
| Self-study Problem preparation Case preparation and Final report |            |    |    |  |  |  |  |  |
|  | evaluation |    |    |  |  |  |  |  |
| 25   | 5          | 20 | 10 |  |  |  |  |  |
| ECTS credits: 3 (90 hours)                                       |            |    |    |  |  |  |  |  |

# **BIBLIOGRAPHY**

# **Basic bibliography**

- Notes prepared by the lecturer (available in Moodle).
- Birge, J.R. and Louveaux, F. (2011) Introduction to Stochastic Programming. Springer-Verlag. Ramos, A., A. Alonso-Ayuso, G. Pérez (eds.) (2008) Optimización bajo Incertidumbre Universidad Pontificia Comillas

# **Complementary bibliography**



|      | IN-CLASS ACTIVITIES |  | OUT-OF-CLASS ACTIVITIES |                         |     | LEARNING<br>OUTCOMES                            |                                  |                  |                       |      |  |
|------|---------------------|--|-------------------------|-------------------------|-----|---|----------------------------------|------------------|-----------------------|------|--|
| Week | h/w                 | LECTURE & PROBLEM SOLVING  | LAB                     | ASSESMENT               | h/w | SELF-STUDY                                      | LAB PREPARATION AND<br>REPORTING | OTHER ACTIVITIES | Learning<br>Outcomes  |      |  |
| 1    | 2                   | Course presentation and topic 1.<br>Introduction to stochastic optimization.<br>Generation expansion planning study<br>case. Production case study. Decision<br>and scenario tree. | Problem solving         |                         |     | Review, self-study and problem-<br>solving (2h) | Problem preparation (1 h)        |                  |                       | RA1. | Understand where to use and concepts of stochastic optimization                        |
| 2    | 2                   | Two-stage and multistage linear optimization. Application to hydrothermal scheduling problem.  | Problem solving         |                         | 4   | Review, self-study and problem-<br>solving (2h) | Problem preparation (2 h)        |                  | RA2, RA3, RA4         | RA2. | Become familiar within the several topics where stochastic optimization can be applied |
| 3    | 2                   | Application case: stochastic unit commitment   | Problem solving         |                         |     | Review, self-study and problem-<br>solving (3h) | Problem preparation (2 h)        |                  | RA2, RA3, RA4         | RA3. | Know how to build an optimization model efficiently                                    |
| 4    | 2                   | Application case: medium-term<br>hydrothermal scheduling   | Case study and practice |                         | 1   | Review, self-study and case-solving (1h)        |                                  |                  | RA5, RA6, RA7         | RA4. | Achieve mathematical rigorousness  |
| 5    | 2                   | Decomposition techniques.  | Case study and practice | Presentation assessment |     | Review, self-study and case-solving (2h)        |                                  |                  | RA5, RA6, RA7         | RA5. | Understand the mathematical techniques used  |
| 6    | 2                   | Linear optimization. Simplex method.<br>Duality.   | Case study and practice |                         | 5   | Review, self-study and case-solving (1h)        | Work preparation (4h)            |                  | RA5, RA6, RA7         | RA6. | State and solve mockup problems  |
| 7    | 2                   | Benders decomposition.   | Case study and practice | Presentation assessment | 2   | Review, self-study and case-solving (2h)        |                                  |                  | RA5, RA6, RA7         | RA7. | Analyze the solutions  |
| 8    | 2                   | Fixed cost transportation problem.   | Case study and practice |                         |     | Review, self-study and case-solving (1h)        | Work preparation (4h)            |                  | RA5, RA6, RA7         | RA8. | Be prepared to extend their knowledge  |
| 9    |                     | Small examples of Benders decomposition.   | Case study and practice | Presentation assessment | 2   | Review, self-study and case-solving (2h)        |                                  |                  | RA5, RA6, RA7         | RA9. | Become familiar with an algebraic language used professionally                         |
| 10   | 2                   | Nested Benders decomposition.  | Case study and practice |                         |     | Review, self-study and case-solving (1h)        | Work preparation (4h)            |                  | RA5, RA6, RA7         |      |  |
| 11   | 2                   | Danztig-Wolfe decomposition.   | Case study and practice | Presentation assessment |     | Review, self-study and case-solving (2h)        |                                  |                  | RA5, RA6, RA7         |      |  |
| 12   | 2                   | Lagrangian relaxation. Fixed cost transportation problem.  | Case study and practice |                         | 5   | Review, self-study and case-solving (1h)        | Work preparation (4h)            |                  | RA5, RA6, RA7         |      |  |
| 13   | 2                   | Scenario tree.   | Case study and practice | Presentation assessment | 7   | Review, self-study and case-solving (2h)        | Final report (5)                 |                  | RA5, RA6, RA7,<br>RA8 |      |  |
| 14   | 2                   | Decomposition in two-stage and multistage stochastic planning.   | Case study and practice |                         | 5   | Review, self-study and case-solving (1h)        | Work preparation (4h)            |                  | RA5, RA6, RA7         |      |  |
| 15   |                     | Improvements in decomposition techniques. Simulation in stochastic programming   | Case study and practice |                         | 7   | Review, self-study and case-solving (2h)        | Final report (5)                 |                  | RA5, RA6, RA7,<br>RA8 |      |  |