

# **GENERAL INFORMATION**

Data of the subject		
Subject name	Differential Equations	
Subject code	DMA-GITI-212	
Mainprogram	Bachelor's Degree in Engineering for Industrial Technologies	
Involved programs	Grado en Ingeniería en Tecnologías Industriales y Grado en Administración y Dirección de Empresas [Second year] Grado en Ingeniería en Tecnologías Industriales [Second year]	
Level	Reglada Grado Europeo	
Quarter	Semestral	
Credits	6,0 ECTS	
Туре	Obligatoria (Grado)	
Department	Department of Applied Mathematics	
Coordinator	Ángela Jiménez Casas	

Teacher Information				
Teacher				
Name	Álvaro Rodríguez Abella			
Department	Department of Applied Mathematics			
EMail	arabella@comillas.edu			
Teacher				
Name	Angela Jiménez Casas			
Department	Department of Applied Mathematics			
Office	Alberto Aguilera 25 [D-202] 2386			
EMail	ajimenez@comillas.edu			
Teacher				
Name	Alicia Castellano García			
Department	Department of Applied Mathematics			
Office	Alberto Aguilera 25 [D-201] 2377			
EMail	acastellano@icai.comillas.edu			
Teacher				
Name	Emanuel Gastón Mompó Pavesi			
Department	Department of Applied Mathematics			
EMail	egmompo@icai.comillas.edu			



Teacher		
Name	Federico Herrero Hervás	
Department	Department of Applied Mathematics	
EMail	fherrero@icai.comillas.edu	

#### **DESCRIPTION OF THE SUBJECT**

# **Contextualization of the subject**

# **Prerequisites**

This course is an introduction to ordinary differential equations (ODEs) and partial differential equations (PDEs). It has two main goals. On the one hand, the course focuses on modelling in terms of ordinary or partial differential equations, a wide variety of problems and phenomena in the fields of physics and engineering. On the other hand, the course focuses on providing the main technical tools and skills for the exact or approximate resolution of such equations. Besides, the stability concept for stationary solutions of nonlinear planar autonomous systems will be studied, in order to obtain qualitative information about the solutions of such kind of systems.

#### **Prerequisites:**

Basic knowledge of linear algebra, geometry and calculus:

- Vector space concept. Coordinates of a vector in a basis. Euclidean vector space concept. Inner products. Orthogonal basis. Eigenvalues and eigenvectors. The Jordan Canonical Form. Affine space concept.
- Explicit, implicit and parametric form of a curve in the plane.
- Geometric interpretation of the derivative and of the partial derivatives. The Chain Rule for derivatives.
- Tangent line and orthogonal line equations to a function in a point of its graph.
- Jacobian Matrix of a vector field.
- Integration: elementary techniques.

### Course contents

# **Contents**

# **Theory**

- 1. First Order Differential Equations.
- 2. Higher Order Linear Differential Equations.
- 3. The Laplace Transform. Operational properties and application to solve initial value problems.
- 4. Linear and Nonlinear Systems of First Order Differential Equations. Stability of critical points of planar autonomous systems.
- 5. Introduction to Fourier expansions. Eigenvalues and eigenfunctions of one-dimensional boundary value problems.
- 6. Introduction to Partial Differential Equations. Evolution PDEs. The Heat Equation and the Wave Equation. The Separation of Variables Method for solving the Heat and the Wave equations in the one-dimensional case. Stationary PDEs. The Laplace/Poisson equations. The Separation of Variables Method for solving the Laplace/Poisson equations in planar domains.
- 7. Numerical solutions to initial and boundary value problems (This part will be developed in two 2-hour laboratory sessions (P1 and P2)).

### Laboratoy



There will be two 2-hour sessions during the semester, between the third and the last lecture week.

- 1. Numerical solutions to initial value problems: Euler Method and Runge-Kutta Method.
- 2. Numerical solutions to one-dimensional boundary value problems: Finite Difference Method.

The laboratory work will be assessed by one 1-hour Lab term exam with Matlab. This lab term exam will consist in obtaining the numerical solutions to some initial and boundary value problems through the implementation with the *Matlab* software of the numerical methods studied in P1 and P2.

#### **EVALUATION AND CRITERIA**

The use of AI to produce full assignments or substantial parts thereof, without proper citation of the source or tool used, or without explicit permission in the assignment instructions, will be considered plagiarism and therefore subject to the University's General Regulations.

Evaluation activities	Evaluation criteria	Weight
<ul> <li>Theoretical-practical exams:</li> <li>Mid term exam (1.5-hour long) (25%)</li> <li>Final term exam (60%)</li> </ul>	<ul> <li>Understanding of concepts</li> <li>Application of concepts, techniques and procedures to problem solving</li> <li>Analysis and interpretation of the results obtained in the resolution of problems</li> <li>Presentation and written communication</li> </ul>	85
Continuous performance evaluation:  • Short continuous assessment tests	<ul> <li>Understanding of concepts</li> <li>Application of concepts, techniques and procedures to problem solving</li> <li>Analysis and interpretation of the results obtained in the resolution of problems</li> <li>Presentation and written communication</li> </ul>	10
Evaluation of the experimental wok:  • Practice exam with MATLAB	<ul> <li>Understanding of concepts</li> <li>Application of concepts, techniques and procedures to practice problem solving</li> <li>Mastery in solving problems with the help of the computer and specific software</li> <li>Analysis and interpretation of the results obtained in the problems solved with a computer</li> </ul>	5

# **Grading**

• The grade obtained in the final exam must be at least 4 over 10 to take into account the previous ponderations of the overall assessment criteria. In other case, the overall grade will be the grade obtained in the exam.



- The following conditions must be accomplished to pass the course:
  - A minimum overall grade of at least 5 over 10.
  - A minimum grade in the final term exam of 4 over 10.

# **BIBLIOGRAPHY AND RESOURCES**

#### **Basic References**

#### **Textbooks:**

- Dennis G. Zill and Warren S. Wright. Differential Equations with Boundary-Value Problems. International Editions. 8th Edt. Brooks/Cole
- William E. Boyce and Richard C. DiPrima. Elementary Differential Equations and Boundary Value Problems. International Student Version. 10th Edt. Wiley.

In compliance with current regulations on the **protection of personal data**, we would like to inform you that you may consult the aspects related to privacy and data that you have accepted on your registration form by entering this website and clicking on "download"

https://servicios.upcomillas.es/sedeelectronica/inicio.aspx?csv=02E4557CAA66F4A81663AD10CED66792