

# **TECHNICAL SHEET OF THE SUBJECT**

Data of the subject		
Subject name	Financial Mathematics	
Subject code	E000005830	
Mainprogram	Bachelor's Degree in Business Administration and Management	
Involved programs	Grado en Administración y Dirección de Empresas (E-2) [Second year] Grado en Administración y Dirección de Empresas y Grado en Derecho (E-3 16) [Second year] Grado en Administración y Dirección de Empresas con Mención en Internacional (E-4) [Second year] Grado en Administración y Dirección de Empresas (E-2) - Bilingüe en inglés [Second year] Grado en Ingeniería en Tecnologías Industriales y Grado en Administración y Dirección de Empresas [Third year]	
Credits	6,0 ECTS	
Туре	Compulsory	
Department	Departamento de Métodos Cuantitativos	
Coordinator	Susana Carabias López	

Teacher Information		
Teacher		
Name	María Elena González Antolín	
Department	Departamento de Métodos Cuantitativos	
EMail	mgantolin@icade.comillas.edu	
Teacher		
Name	María Jesús Espinosa Jiménez	
Department	Departamento de Métodos Cuantitativos	
EMail	mjespinosa@icade.comillas.edu	
Teacher		
Name	Óscar Díez Alonso	
Department	Departamento de Métodos Cuantitativos	
EMail	odiez@icade.comillas.edu	
Teacher		
Name	Raquel Redondo Palomo	
Department	Departamento de Métodos Cuantitativos	
Office	Alberto Aguilera 23 [0D-221]	
EMail	rredondo@icade.comillas.edu	
Phone	2299	
Teacher		
Name	Francisco de Asís de Ribera Martín	



Departamento de Métodos Cuantitativos		
fadribera@comillas.edu		
Teacher		
Juan Ignacio García Pérez de la Blanca		
Departamento de Gestión Financiera		
jigarcia@icade.comillas.edu		
Laura Palacio Aragón		
Departamento de Métodos Cuantitativos		
lpalacio@icade.comillas.edu		
Teacher		
María Eugenia Fabra Florit		
Departamento de Métodos Cuantitativos		
Alberto Aguilera 23		
mefabra@icade.comillas.edu		
2239		

# SPECIFIC DATA OF THE SUBJECT

## **Contextualization of the subject**

## Contribution to the professional profile of the degree

The subject is designed to provide students with the knowledge and the resources that are needed to analyze and compare financial operations that are held in an environment characterized by certainty, as well as the foundations to solve problems associated with many kinds of financial transactions.

## Prerequisites

Mathematics at high school level.

Competencies - Objectives		
Competences		
GENERALES		
CG01	Capacidad de análisis y síntesis	
	RA1	Capacidad para expresarse en lenguaje matemático
	RA3	Identifica estructuras comunes en situaciones reales diferentes



CG02	Resolución de problemas y toma de decisiones	
	RA1	Capacidad para la formulación en lenguaje matemático de los problemas que surgen en la gestión empresarial y de la resolución de los mismos
CG04	Capacidad de gestionar información proveniente de fuentes diversas	
	RA1	Capacidad de búsqueda y selección de bibliografía adecuada y otras fuentes para documentarse sobre un contenido concreto
CG14	Capacidad para aprender y trabajar autónomamente	
	RA2	Desarrolla habilidades necesarias para el estudio e investigación independiente
ESPECÍFICAS		
	Conocimiento de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico- empresarial	
CE08	Conocimientc empresarial	o de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico-
CE08	Conocimiento empresarial RA1	o de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico- Aplica la abstracción la simplificación para modelar en términos matemáticos el problema al que se enfrenta
CE08	Conocimiento empresarial RA1 RA2	Aplica la abstracción la simplificación para modelar en términos matemáticos el problema al que se enfrenta Conoce los instrumentos matemáticos necesarios para la modelización
CE08	Conocimiento empresarial RA1 RA2 RA9	<ul> <li>de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico-</li> <li>Aplica la abstracción la simplificación para modelar en términos matemáticos el problema al que se enfrenta</li> <li>Conoce los instrumentos matemáticos necesarios para la modelización</li> <li>Conoce las variables y funciones más relevantes en la valoración de mercados de renta fija</li> </ul>
СЕ08 СЕ09	Conocimiento empresarial RA1 RA2 RA9 Comprensión	<ul> <li>de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico-</li> <li>Aplica la abstracción la simplificación para modelar en términos matemáticos el problema al que se enfrenta</li> <li>Conoce los instrumentos matemáticos necesarios para la modelización</li> <li>Conoce las variables y funciones más relevantes en la valoración de mercados de renta fija</li> <li>y correcta aplicación de los modelos matemáticos dinámicos y de valoración financiera</li> </ul>
CE08 CE09	Conocimiento empresarial RA1 RA2 RA9 Comprensión RA1	<ul> <li>de técnicas matemáticas que permiten modelizar y resolver problemas en el ámbito económico-</li> <li>Aplica la abstracción la simplificación para modelar en términos matemáticos el problema al que se enfrenta</li> <li>Conoce los instrumentos matemáticos necesarios para la modelización</li> <li>Conoce las variables y funciones más relevantes en la valoración de mercados de renta fija</li> <li>y correcta aplicación de los modelos matemáticos dinámicos y de valoración financiera</li> <li>Conoce y sabe aplicar los conceptos de ley financiera y equivalencia financiera</li> </ul>

# THEMATIC BLOCKS AND CONTENTS

Contents - Thematic Blocks		
BLOCK 1: FUNDAMENTAL ELEMENTS OF FINANCIAL MATHEMATICS		
Topic 1: FINANCIAL CAPITALS AND FINANCIAL OPERATIONS		
<b>1.1</b> Financial capital: definition and unit of measure		
1.2 Financial operations: definition		
<b>1.3</b> Financial operations: classification		
Topic 2: FINANCIAL LAWS		
2.1 Financial law as a criteria to project financial capitals		





2.2 Commonly used laws of accumulation

#### 2.3 Commonly used laws of discount

#### Topic 3: FINANCIAL EQUILIBRIUM

- 3.1 The equation of financial equivalence
- 3.2 The financial equilibrium of a financial operation
- 3.3 Income and effective rates. The rules of the Spanish Central Bank: TAE
- 3.4 Outstanding balance. Definition and calculation methods

#### **BLOCK 2: FINANCIAL OPERATIONS IN THE LONG RUN**

#### Topic 4: VALUATION OF ANNUITIES

4.1 Annuities: definition and classification

- 4.2 The value of constant annuities
- **4.3** The value of variable annuities
- 4.4 Application to financial decisions. NPV and IRR

#### Topic 5: PRIVATE LOANS

- 5.1 Concept and general overview
- 5.2 Classical amortization methods
- 5.3 Mortgage loans

#### **BLOCK 3: INTRODUCTION TO MARKET VALUATION**

#### Topic 6: OPERATIONS WITHIN "FIXED INCOME" MARKETS

- 6.1 Public promissory notes (Treasury Bills)
- 6.2 Government bonds
- 6.3 The market value of a loan
- 6.4 The term structure of interest rates (TTIR)

## **TEACHING METHODOLOGY**

#### General methodological aspects of the subject

### In-class Methodology: Activities

**Master class:** The teacher will explain the subject's basic concepts as well as the relationships between them, with emphasis on the fact that the same principles can be applied to study a wide range of financial operations. The material explained in each class will be based on the material taught in the previous ones; for this reason, to obtain the best results it is key to deeply assimilate previously learnt concepts.





In addition, the student is recommended to bring to each class the corresponding material.

**Practical class:** In each session we will discuss the exercises that the student worked out at home and we will present new probems to be solved in class. Quizzes will be administered as independent activities. The work may be submitted upon teacher's request at the end of a class. Students are expected to actively participate in the practical sessions with an adequate knowedge of the material, which will contribute to the student's overall score on the subject

**Midterm exams:** depending of the topic, midterm exams will have different formats and be more or less comprehensive; they will be designed to assess the student's understanding of the subject

#### **Non-Presential Methodology: Activities**

**Preparation for the master class:** At the end of each class, students are supposed to self-assess what they have learned and supplement it with the provided material. Students not achieving an optimum performance in the master class will be expected to talk to their teacher in order to identify the sources of their problem.

**Preparation for the practical class:** Before each practical class, students are expected to solve the exercises previously pointed out by the instructor .

**Preparation and analisis of midterm exams:** At the end of each topic, the student is expected to review all the concepts that they have learned and understand the relationships that exist between them and with the concepts learned in previous topics. When the student receives a graded test they should critically analyze their mistakes and talk to the professor in case the score does not correspond with their expectations.

**Assignment I:** once having made a group of three, the students are expected to select an actual loan and analyze it. They are expected to submit two reports, one at the beginning of the course and another at the end, by so reflecting their understanding progress.

**Assignment II (non-mandatory):** The students are expected to compare the presentation of a key concept of financial mathematics done in the basic bibliography with another source of their choice. Then, they are expected to produce a report based on this comparison.

Assignment III and IV (non-mandatory): The students are expected to apply the concepts of annuities to financial valuation problems, using the spreadsheet Excel.

## SUMMARY STUDENT WORKING HOURS

CLASSROOM HOURS				
Lecciones de carácter expositivo	Ejercicios y resolución de casos y de problemas			
36.00	24.00			
NON-PRESENTIAL HOURS				
Estudio individual y/o en grupo y lectura organizada	Ejercicios y resolución de casos y de problemas	Trabajos monográficos y de investigación, individuales o colectivos		
50.00	35.00	10.00		
		ECTS CREDITS: 6,0 (155,00 hours)		





# **EVALUATION AND CRITERIA**

Evaluation activities	Evaluation criteria	Weight
Tests for all groups in each specialty	<ul> <li>To understands concepts</li> <li>To properly apply these concepts to solve the problems that relate to financial operations</li> </ul>	75 %
Continuous evaluation exams	<ul> <li>To understands concepts</li> <li>To properly apply these concepts to solve the problems that relate to financial operations</li> </ul>	10 %
Assignments	<ul> <li>To identify quality information</li> <li>To identify the relevant information for a given problem</li> <li>To correctly interpret the information provided by a financial institution</li> <li>To correctly apply the concepts related to specific loans</li> <li>To learn how to quote and reference properly</li> <li>To develop concepts and conclusions by using a language that is consistent with what is required</li> <li>To properly use the spreadsheet Excel to apply theoretical concepts</li> </ul>	10 %
Active involvement/Class participation	<ul> <li>To correctly perform the required work</li> <li>To actively participate in class activity</li> </ul>	5 %

# Ratings

Evaluation rules are described in the following paragraphs. Each activity includes in parenthesis their weight in the student's overall course scores. These weights are applicable to students who enrolled for the first time (i.e. first call, en su primera convocatoria).

For students in their second or higher call (tercera convocatoria o superiores), or students with attendance waiver (dispensa de escolaridad), the course score will be the maximum between the final exam score and the score describe beforehand for students first-time enrolled (the latter will ONLY be applied to the activities that the student will decide to undertake).

Final exam (65%-75% Favorable compensation with continuous evaluation)

The purpose is to verify whether the student understands and manages the basic concepts that were explained during the classes, as well as to verify whether he/she is able to apply them to the analysis of the financial operations that were discussed during the course.

The final exam will be the same (and will be offered on the same date and time) of the remaining students of the same degree study.





#### Continuous evaluation exams (10%-20% Favourable compensation with final exam)

During the class time and on the dates announced in class, there will be three short midterm exams. The topics that will be covered in each midterm exam will focus on the concepts that teacher expects to be managed by the students on a normal understanding of the subject. Midterms exams will under no circumstances be repeated and students not taking the exam gets a zero score for that midterm exam. Subject to teacher's unquestionable opinion and provided a justifiable reason, the zero score earned in that exam might be excluded from the student's continuous evaluation score.

**Assignments** (10%) Students are expected to submit on, two extensive reports (the first report will be submitted again as a third revised assignment) focusing of the search and the analysis of financial information, Please see details on the documents that are available in Moodle. They can also submit three non mandatory reports which will be considered to improve assignments grade.

Active involvement / Class participation (5%): Another component of student's final evaluation will be their active involvement in classroom activities (such as asking question related to the subject, answering teacher's questions or solving exercises on the blackboard). Teacher may ask, at any time, to submit the exercises that were requested to the students in advance. This section of the evaluation is not focused on accurate figures but on the proactive, constant and regular work of the student.

## WORK PLAN AND SCHEDULE

Activities	Date of realization	Delivery date
Assignment 1. Initial report.	week 2	week 2 or 3
Assignment 2 (non-mandatory)	Between week 2 and 5	Between week 3 and 6
Assignments 3 and 4 (non-mandatory)	Between week 9 and 12	week 11 or 12
Assignment 1. Final report.	week 12 and 13	week 13 or 14

## **BIBLIOGRAPHY AND RESOURCES**

#### **Basic Bibliography**

TEXTBOOK

Bonilla Musoles, MA, Ivars Escortell, AN & Ismael Moya CL 2006, Matemática de las operaciones financieras: teoría y práctica, Thomson, Madrid.

Kellison, ST 2009, The theory of interest. McGraw-Hill, New York

WEB SITES

Banco de España: http://www.bde.es/

Tesoro Público: http://www.tesoro.es/



## **Complementary Bibliography**

TEXTBOOKS:

Bonilla Musoles, MA & Ivars Escortell, MA 1994, Matemáticas de las operaciones financieras : (teoría y práctica), AC, Madrid.

Broverman, S.A., 2017 Mathematics of Investment and Credit, ACTEX

Francis, J. and Ruckman, C., 2018, Interest Theory – Financial Mathematics and Deterministic Valuation, ActuarialBrew

Gil Peláez, LO, Baquero, MJ, Gil, MA & Maestro, ML 1991, Matemática de las operaciones financieras: problemas resueltos, AC, Madrid.

Pablo López, AN 2000, Manual práctico de matemática comercial y financiera, Centro de Estudios Ramón Areces, Madrid.

Pablo López, AN 2002, Valoración financiera, Centro de Estudios Ramón Areces, Madrid.

Pablo López, AN de 2003, Matemática de las operaciones financieras I, UNED, Madrid.

Vaaler, L.J.F., Harper, S.K. & Daniel, J.W. Mathematical Interest Theory (Third Edition), 2019, The Mathematical Association of America

In compliance with current regulations on the **protection of personal data**, we would like to inform you that you may consult the aspects related to privacy and data <u>that you have accepted on your registration form</u> by entering this website and clicking on "download"

https://servicios.upcomillas.es/sedeelectronica/inicio.aspx?csv=02E4557CAA66F4A81663AD10CED66792