



GRADO EN INGENIERÍA EN TECNOLOGÍAS
INDUSTRIALES

TRABAJO FIN DE GRADO

ANALYSIS IN AIRFIELD CAPACITY AND DELAY

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Madrid

Julio de 2019

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Analysis in Airfield Capacity and Delay

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ANALYSIS IN AIRFIELD CAPACITY AND DELAY

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Madrid

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ÁNÁLISIS DE LA CAPACIDAD AÉREA Y TIEMPO DE ESPERA PARA ATERRIZAJES BASADOS EN EL MÉTODO DE GRUPOS

Autor: **Navascués Gómez, Juan Lorenzo de.**

Director: Schonfeld, Paul M.

Entidad Colaboradora: University of Maryland / ICAI – Universidad Pontificia Comillas.

RESUMEN DEL PROYECTO

Introducción:

La industria aérea está experimentando un continuo crecimiento y desarrollo a nivel mundial. El número de pasajeros y vuelos que se producen diariamente aumenta año tras año. De acuerdo a la Administración Federal de Aviación de los Estados Unidos (FAA), la aviación y en especial, el flujo de pasajeros ha experimentado un crecimiento constante durante los últimos 10 años y se espera que continúe en el futuro próximo. Además, cálculos y estudios realizados por la Asociación Internacional de Transporte Aéreo (IATA) pronostican que, siguiendo la tendencia de los últimos años, en 2037 el número de pasajeros podría doblarse hasta los 8.200 millones.

Esta evolución y aumento de la demanda exige a los aeropuertos un continuo desarrollo y evolución para poder hacer frente a las nuevas necesidades. Sin embargo, los aeropuertos no pueden crecer ni aumentar el tamaño de sus instalaciones de igual manera y velocidad que la demanda. Por esto, paralelamente a este crecimiento se está produciendo el aumento en niveles de tráfico aéreo generando un mayor número de situaciones de congestión aérea¹. De este modo, los aeropuertos además de realizar las mejoras necesarias y alcanzables en términos de infraestructura e instalaciones, necesitarán modificar y analizar sus modelos operativos para hacer frente a este crecimiento y mejorar en otros aspectos como la capacidad aeroportuaria².

¹ Un aeropuerto se encuentra en congestión aérea cuando no es capaz de realizar el número de operaciones (despegues y/o aterrizajes) demandadas en un determinado intervalo de tiempo.

² La capacidad aeroportuaria se define como el rendimiento máximo sostenible de las operaciones de aterrizajes y/o despegues que se pueden lograr en un intervalo de tiempo específico con un nivel de retraso aceptable.

Por todo lo anterior, este proyecto se centra en analizar y determinar si el modelo de operación utilizado en la distribución de aeronaves en el momento de aterrizaje puede verse mejorado por los aterrizajes basados en el método de grupos.

Actualmente los aeropuertos operan siguiendo el First-Come, First-Serve (F.C.F.S.) que se basa en otorgar permiso para aterrizar a las aeronaves según el orden en el que éstas lo piden. Como resultado, surge un orden completamente aleatorio de aeronaves aterrizando sin tener en cuenta tamaños y velocidades de acercamiento. La Organización de Aviación Civil Internacional (ICAO) divide las aeronaves en 4 grupos diferentes teniendo en cuenta su velocidad de aproximación y el vórtice que generan:

Tipo de Aeronave	Velocidad de acercamiento (KNOTS)	Velocidad Máxima para Circling	Vórtice Generado	Aeronave Tipica
A	<91	100	Small	Small Single engine
B	91-120	135	Small	Small Multi engine
C	121-140	180	Large	Airline Jet
D	141-165	205	Heavy	Large Jet/Military Jet

Tabla 1 Clasificación de Aeronaves según Velocidad de Acercamiento y Vórtice

Fuente: ICAO

Aunque el FCFS no considera el tipo de aeronave entrante, las regulaciones existentes sí determinan un espacio mínimo de seguridad entre cada aterrizaje que depende principalmente del tamaño y vórtice generado por el aterrizaje precedente. De acuerdo a la regulación estadounidense, estas distancias (en millas náuticas) deben ser:

Leading Aircraft	Nautical Miles	Trailing Aircraft		
		Heavy	Large	Small
	Heavy	4	5	5/6*
	Large	2.5 (or 3)	2.5 (or 3)	3/4*
	Small	2.5 (or 3)	2.5 (or 3)	2.5 (or 3)

Tabla 2 Separación Mínima entre aterrizajes consecutivos

Fuente. FAA

Como consecuencia, el FCFS no optimiza el orden de llegada de tal forma que se produzca el mínimo tiempo entre dos aterrizajes consecutivos y reducir así el tiempo total de operaciones.

El método de grupos se basa en realizar los aterrizajes en ciclos de intervalos de escuadrones de aviones según su tamaño y/o velocidad de aproximación. De esta manera, se busca conseguir reducir al máximo el número de aterrizajes que preceden a aeronaves de diferente categoría. Como resultado, se obtendría un mayor número de operaciones alcanzables y se reducirían las situaciones de congestión aérea.

El siguiente diagrama espacio tiempo muestra un cómo sería un ciclo del FCFS y cómo sería un ciclo del método de escuadrones:

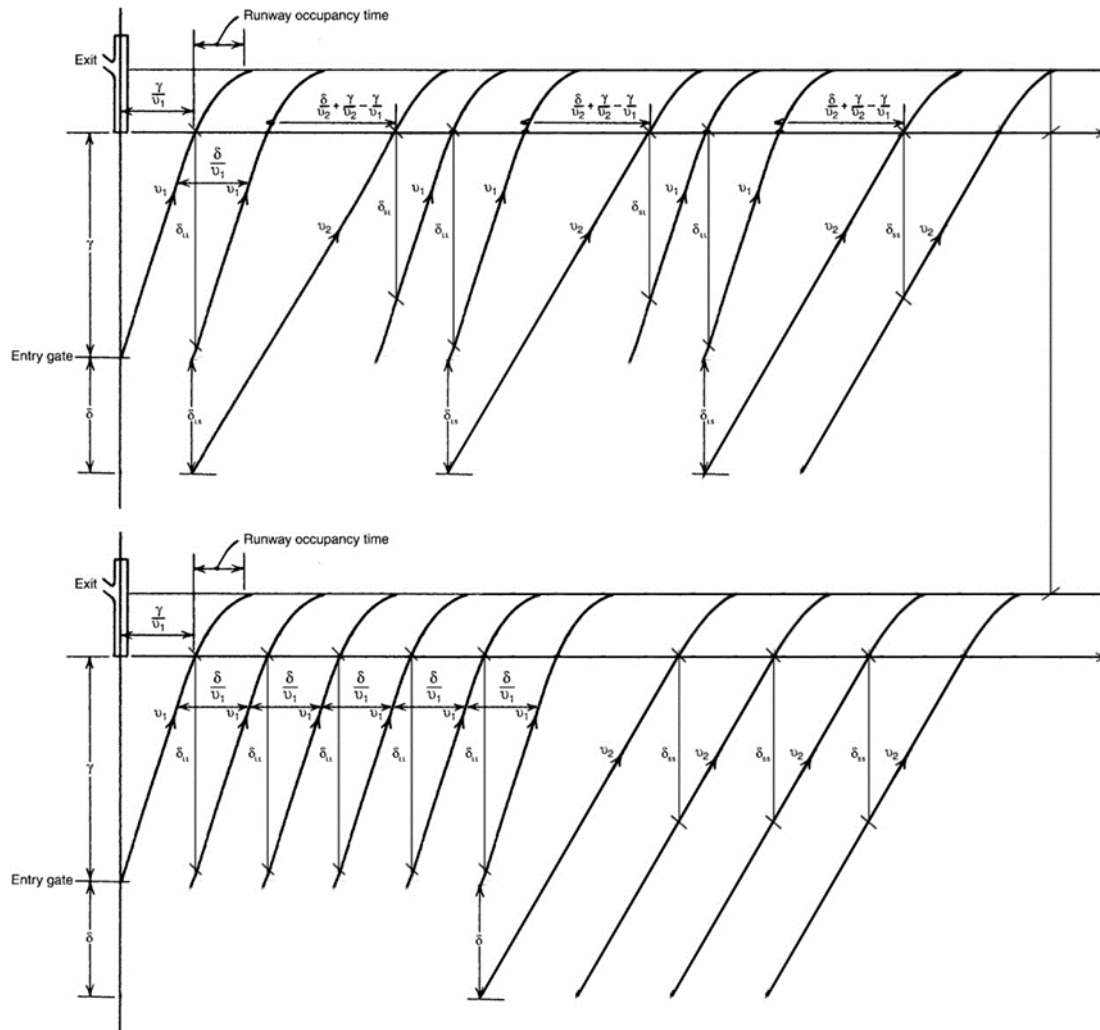


Figura 1 Comparación de llegadas siguiendo el FCFS y el método de grupos.

Fuente: Elaboración Propia

Metodología:

El objetivo de este proyecto es determinar si como primer análisis, el método basado en grupos proporciona mejores resultados en términos de capacidad que los obtenidos con el FCFS. Para conseguir este análisis, se ha desarrollado la formulación para el método basado en grupos considerando velocidades de aproximación, separaciones mínimas de acuerdo a la regulación y probabilidades de aeronaves de acuerdo a las establecidas por

la FAA. Además, se ha analizado también como afectaría al tiempo medio de retraso la incorporación de este método desarrollando una formulación basada en la probabilidad de que cada grupo se encuentre en su turno de aterrizaje y tiempo medio de espera. Todos estos cálculos, se han comparado con los resultados del FCFS para los mismos escenarios. Para los cálculos del FCFS se ha seguido la formulación establecida por (Norman J. Ashford, 2011) y para el cálculo del tiempo de retraso medio, se utilizó la fórmula de Pollaczek–Khinchine³. Como herramienta de resolución para los diferentes casos analizados, se ha utilizado Excel introduciendo todas las variables y constantes determinantes. Además, se ha desarrollado una macro en Excel que contiene dos programas de análisis. El primero permite al usuario introducir una serie de datos específicos en relación a la velocidad de acercamiento y el número de mezclas de aeronaves que quiere comparar. Como resultado, el programa generará X mezclas de aeronaves aleatorias, y comparará los resultados con los del FCFS otorgando como salida gráficos de comparación entre los dos métodos. El segundo programa, permite al usuario introducir 3 casos específicos que quiera comparar o comprobar diferencias y proporciona como salida una matriz de gráficos en la que se muestra los análisis más importantes.

En este proyecto, se ha analizado también la posibilidad de añadir despegues entre medias de los aterrizajes del método de grupos lo que proporcionaría un aumento extra en la capacidad del aeropuerto. Todos los escenarios y cálculos se han realizado para aeropuertos con una pista de aterrizaje como el Aeropuerto Internacional de San Diego:

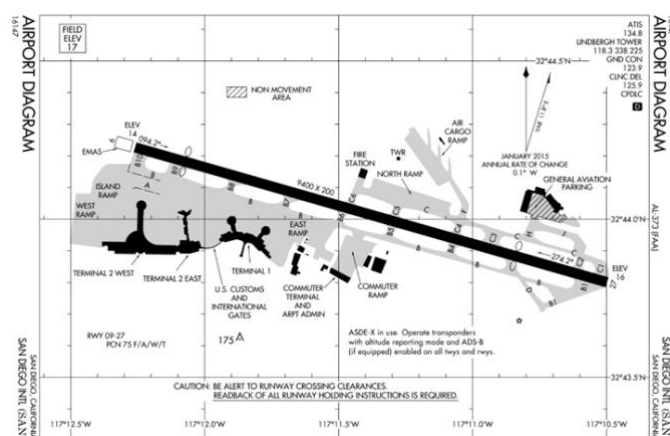


Figura 2 Plano Aeropuerto Internacional de San Diego

Fuente: FAA

³La fórmula de Pollaczek-Khinchine, establece una relación entre la longitud media de la cola y el tiempo medio de espera o servicio del modelo analizado

Resultados:

Caso Base:

- 2 tipos de aviones y Aircraft Mix A:40% B:0% C:60% D:0%
- 4 tipos de aviones y Aircraft Mix A:20% B:40% C:20% D:20%

En este caso base se realizaron los análisis y comparación entre las mezclas de aeronaves anteriormente expuestas y se obtuvieron los siguientes resultados:

(Cabe mencionar que “Mixed Arrivals” hace referencia al FCFS y “Grouping Method” al método basado en escuadrones o grupos de aviones).

Capacidad:

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	30.53 ops/hour	40.51 ops/hour
A:20% B:40% C:20% D:20%	31.40 ops/hour	34.53 ops/hour

Tabla 3 Resultados para la Capacidad Caso Base

Tiempo de espera medio:

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	25.35 secs/op	42.8 secs/op
A:20% B:40% C:20% D:20%	26.57 secs/op	45.35 secs/op

Tabla 4 Resultados tiempo de espera medio Caso Base

Despegues Intermedios Aterrizajes:

Aircraft Type		Leading Aircraft	
		A	C
Trailing Aircraft	A	NO	SÍ
	C	NO	NO

Tipo de Aeronave		Avión Precedente			
		A	B	C	D
Avión que Sigue	A	NO	SÍ	SÍ	SÍ
	B	NO	NO	SÍ	SÍ
	C	NO	NO	NO	SÍ
	D	NO	NO	NO	NO

Tabla 5 Resultados Despegues Caso Base

Extensión Caso Base:

Como extensión del caso base, se procedió a realizar un análisis de 5 escenarios diferentes que representan de una manera más fiable los resultados del método basado en escuadrones. Los 5 escenarios se eligieron de acuerdo a la formulación de la FAA. Los resultados de la comparación entre los 5 escenarios con el método de escuadrones y el FCFS pueden verse en los gráficos siguientes:

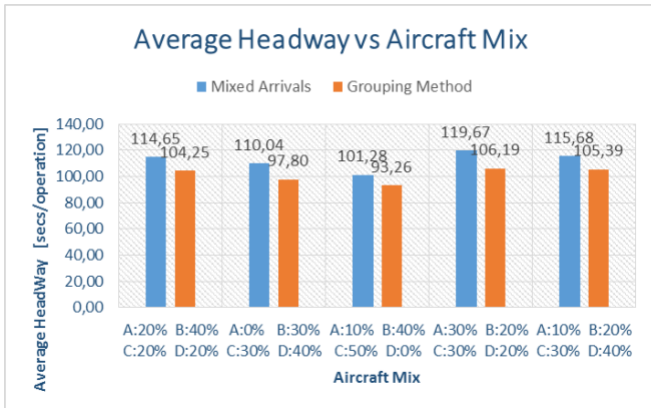


Figura 4 Frecuencia Media de Aterrizajes VS Mezcla de Aviones

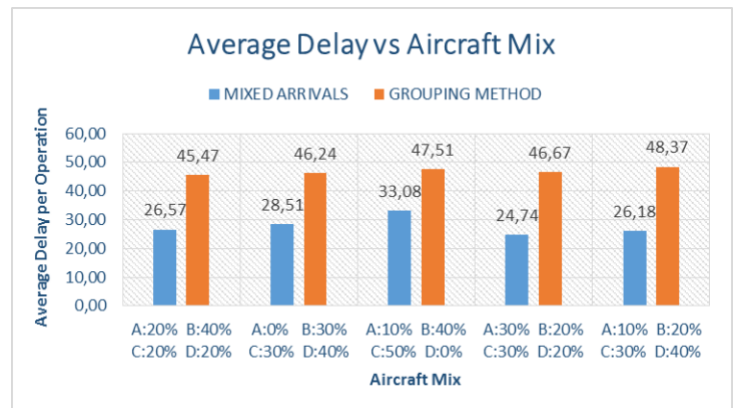


Figura 3 Tiempo Medio de Espera VS Mezcla de Aviones

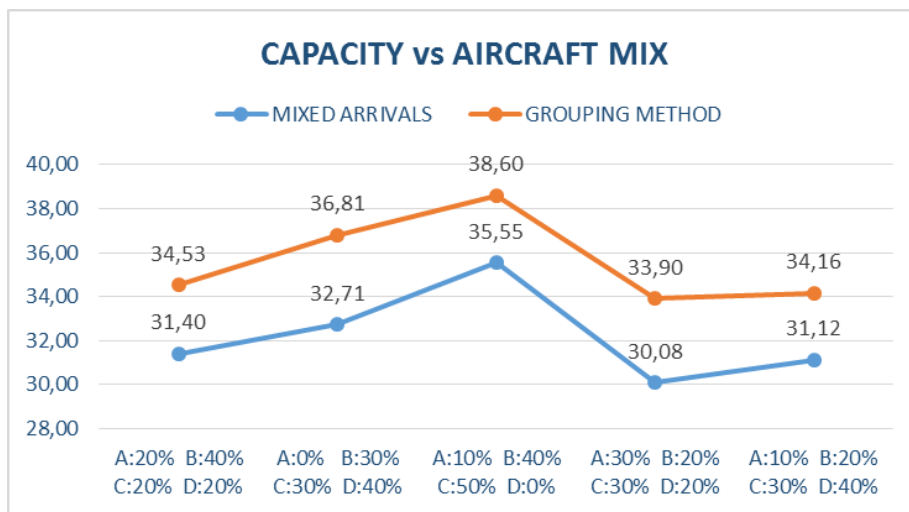


Figura 5 Capacidad VS Mezcla de Aviones

Además, se realizó un estudio sobre la influencia que tiene el tamaño del ciclo dentro del método de escuadrones. Es decir, cómo influye el número de aviones que aterrizan por cada ciclo del método de escuadrones.

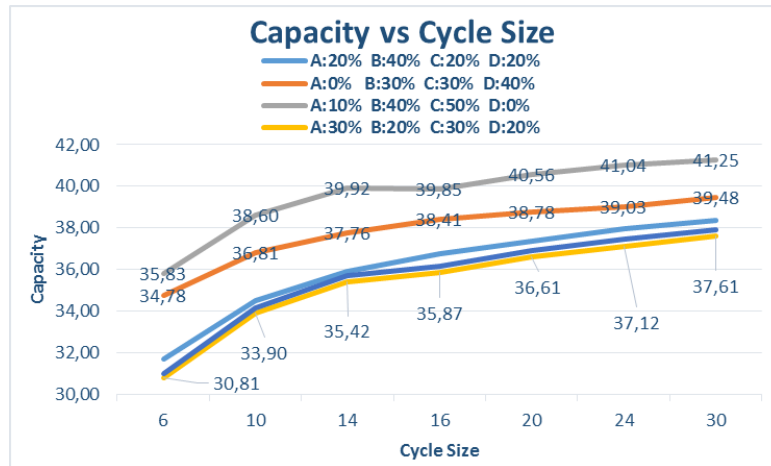


Figura 6 Capacidad VS Aterrizajes por ciclo

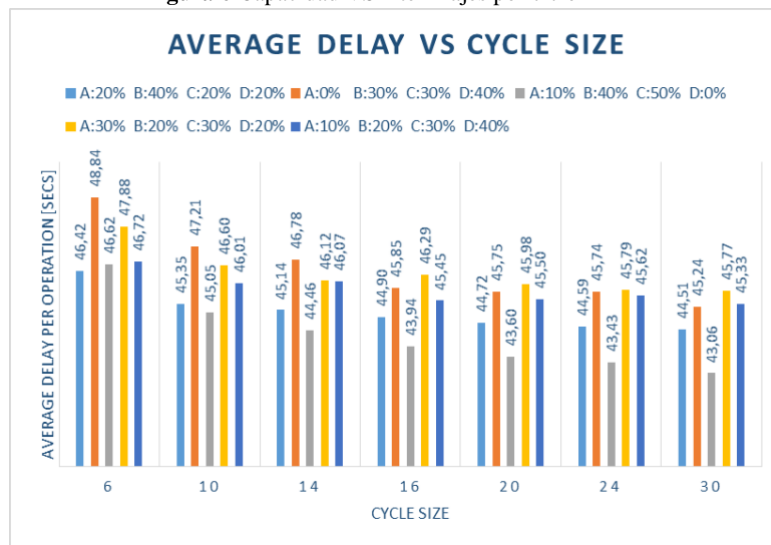


Figura 7 Tiempo medio de espera VS Aviones por ciclo



Figura 8 Análisis individual tiempos de espera medios VS Aviones por ciclo para cada escenario

Conclusiones:

La industria de la aviación va a tener que hacer frente a un continuo aumento de la demanda que supondrá una mayor exigencia a los aeropuertos en todos los ámbitos. Con los resultados del análisis realizado en este proyecto, se puede concluir que una primera solución para enfrentarse a las situaciones de congestión aérea es la aplicación del método de grupos/escuadrones de aviones y la aplicación de los despegues entre aterrizajes consecutivos. No obstante, en vista de los resultados obtenidos, la aplicación de este nuevo método no tiene sentido en situaciones no congestionadas. En todos los casos analizados tanto en este proyecto como en la herramienta Excel desarrollada, la capacidad aeroportuaria aumenta con el método de escuadrones pero el tiempo medio de espera también lo hace, provocando que el FCFS sea el mejor método para situaciones de no congestión (pues la demanda es inferior a la capacidad que éste puede ofrecer).

Como conclusión final, se debe decir que el método de escuadrones o grupos supone en primera instancia, una mejora de la capacidad en todos los niveles. Por ello, debería ser analizado con la tecnología y software utilizados en las instalaciones de los aeropuertos. Asimismo, sería óptimo desarrollar un software que permitiese a los controladores cambiar de método de forma dinámica en el momento en el que se necesite hacer frente a una demanda mayor de la alcanzable por el FCFS y la utilización del método de escuadrones fuese mejor. Cabe decir que en este análisis se han realizado aproximaciones razonables y por tanto, los futuros análisis que se realicen con instrumentos y tecnología real deberían considerar todos los factores adyacentes como taxiways, touchdowns, o aproximaciones erróneas.

ANALYSIS IN AIRFIELD CAPACITY AND DELAY FOR THE GROUPING METHOD

Introduction:

The aviation industry is experiencing constant growth and development worldwide. The number of passengers and flights increases from year to year. According to the FAA (Federal Aviation Administration), aviation and, in particular, passenger flow have been growing at a constant rate for the last 10 years and this growth is expected to continue for the upcoming future. Furthermore, IATA (International Air Traffic Transportation) forecast shows that present trends in air transportation suggest passenger flow could double actual levels rising them up to 8.2 billion in 2037.

This growth in passenger flow will make major changes in demand, forcing airports to continuously develop improvements to meet the growing demand. However, airports cannot modify its layout, or increase their area at the same speed as the demand grows. This situation leads us to a scenario where air traffic keeps growing resulting in more congested periods for the airports. In this way, airports will need to modify and update their operating systems to face this demand by increasing its actual airfield capacity.

In this light, this Project is focused on analyzing and determining whether the actual operating system used for landings could be improved by arrivals following the grouping method.

Currently, airports operate landings following the First-Come, First-Serve (FCFS) method basis where aircraft lands according to the order in which they have asked for permission. This method is probably the most effective and the best one for non-congested periods. However, at times when the airports are suffering from air traffic congestion (which will be very likely to happen at the growth rates we are currently experiencing), there is room for improvement in the FCFS, as we will discuss in this paper.

As a result of this method, a completely random order of arrivals come up without considering aircraft size or approaching speeds. According to ICAO (International Civil Aviation Organization), there are 4 different aircraft class considering its approaching speed and maximum take-off weight (MTOW) classification:

Aircraft Class	Approaching speed (KNOTS) V_{AT}	Maximum speeds for circling	Wake Turbulence Classification	Typical aircraft in this category
A	<91	100	Small	Small Single engine
B	91-120	135	Small	Small Multi engine
C	121-140	180	Large	Airline Jet
D	141-165	205	Heavy	Large Jet/Military Jet

Table 1 Aircraft Classification According Approaching Speed

Source: ICAO

Although the FCFS does not consider the aircraft classification of the upcoming arrival, existing regulations established by the FAA determine a minimum safety separation between two consecutive landings according to its classification and wake vortex generated:

Leading Aircraft	Nautical Miles	Trailing Aircraft		
		Heavy	Large	Small
Heavy		4	5	5/6*
Large		2.5 (or 3)	2.5 (or 3)	3/4*
Small		2.5 (or 3)	2.5 (or 3)	2.5 (or 3)

Table 2 Minimum Safety Separation between two consecutive Arrivals

Source:FAA

As a result, the FCFS does not optimize the arrival order in a way which the time between two consecutive arrivals is the minimum and reducing the total operational time per cycle. On the other hand, the grouping method will divide the upcoming arrivals into cycles of platoons of the same aircraft class and approach speed in order to reduce the time between each. In consequence, the airfield capacity would increase and the number of congested periods would become lower.

The following time-space diagram compares how a landing cycle would be using the FCFS and the grouping method for two different types of aircraft.

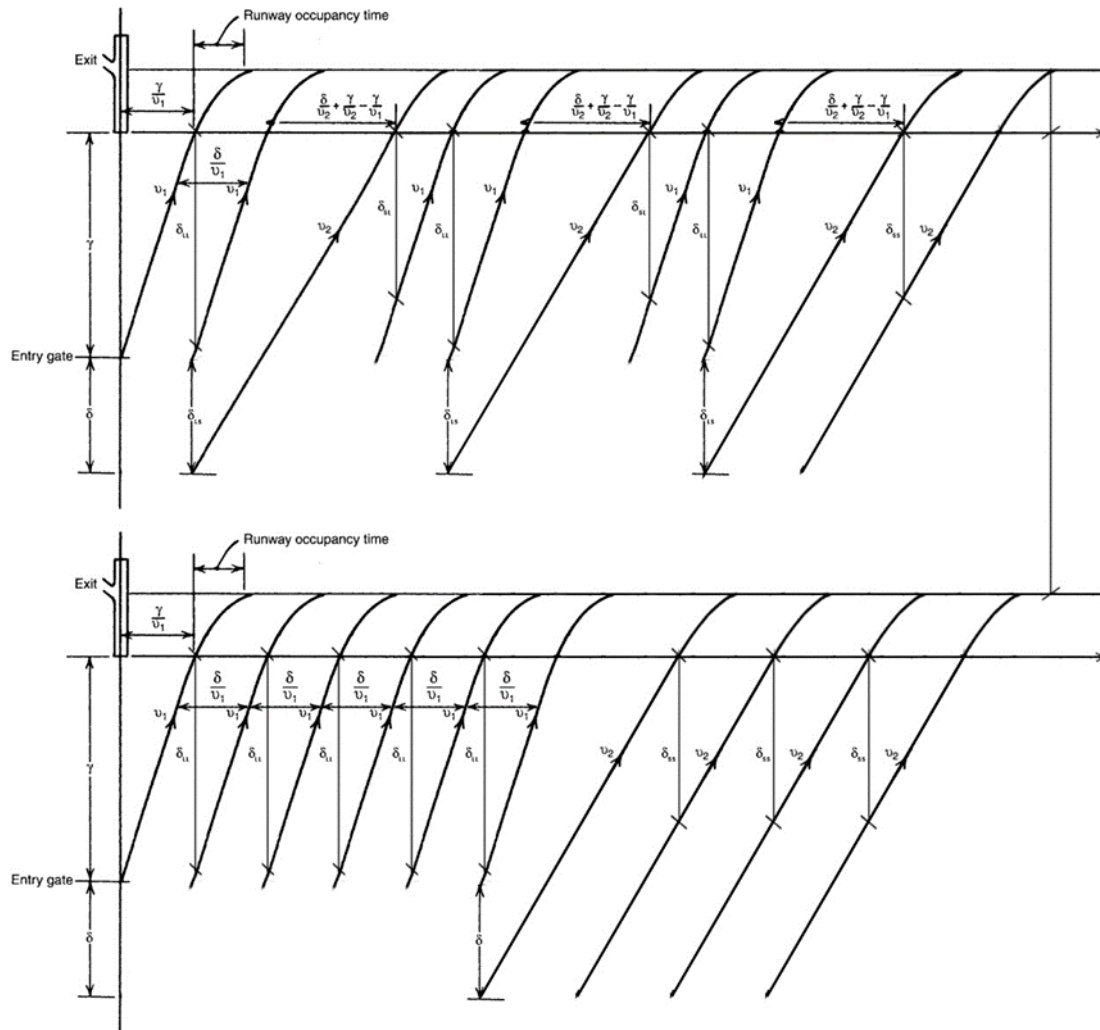


Figure 1 Time-Space diagram for FCFS & the Grouping Method Source:Prepared by the author

Methodology:

The ultimate goal of this paper is to determine as a first approach, whether the grouping method provides better results in airfield capacity than the FCFS or not. To achieve this, we have developed the formulation for this method considering approaching speeds, minimum safety separations, and aircraft mix according to the FAA regulations. In addition, the average delay this method would cause has been analyzed and properly compared to the FCFS. For this formulation, it has been assumed a total waiting time of half of the duration of its platoon in the case the plane arrives at the same time its platoon has obtained permission to begin landing. Otherwise, if the plane arrives when a different group is landing, it will have to wait for the duration of all the others platoons plus half of its own. This a simple and conservative way of calculating the average delay that will give us a reasonable approach and comparison to the mixed one. For the FCFS calculations, it has been used the Pollaczek–Khinchine queuing theory. All calculations

have been computed by means of Excel. Additionally, two programs have been coded in Excel. In the first one, the user inputs the specific data (approaching speed, length of common approach) and the number of different he wants to analyze. As a result, the program will output three charts comparing the different aircraft mixes using the Grouping Method to the FCFS. The second program allows the user to input three specific mixes and it will output nine charts to compare the results between them and the FCFS.

In this project, the possibility of incorporating take-offs between two consecutive landings in the grouping method has been also analyzed. In the cases where this is reachable, it will mean an extra addition in terms of airfield capacity. All calculations and scenarios alongside this paper have been computed for an airport of one runway (i.e. San Diego Int. Airport).

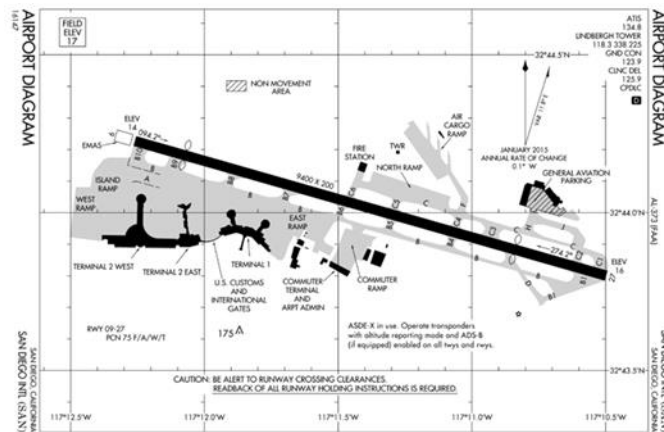


Figure 2 San Diego International Airport Layout

Source:FAA

Results:

Case Study:

- 2 Aircraft Types & Aircraft Mix A:40% B:0% C:60% D:0%
- 4 Aircraft Types & Aircraft Mix A:20% B:40% C:20% D:20%

In this initial case, the above-stated aircraft mixes have been analyzed to establish a comparison between the two methods of allocating arrivals:

Capacity:

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	30.53 ops/hour	40.51 ops/hour
A:20% B:40% C:20% D:20%	31.40 ops/hour	34.53 ops/hour

Table 3 Capacity Results for the Case Study

Average Delay:

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	25.35 secs/op	42.8 secs/op
A:20% B:40% C:20% D:20%	26.57 secs/op	45.35 secs/op

Table 4 Average Delay Results for the Study Case

Takeoffs between Consecutive Landings:

Aircraft Type		Leading Aircraft	
		A	C
Trailing Aircraft	A	NO	YES
	C	NO	NO

Aircraft Type		Leading Aircraft			
		A	B	C	D
Trailing Aircraft	A	NO	YES	YES	YES
	B	NO	NO	YES	YES
	C	NO	NO	NO	YES
	D	NO	NO	NO	NO

Table 5 In-between Takeoffs Results for the Case Study

Case Study Extension:

As an extension for the basic case, an analysis for 5 different scenarios was developed in order to obtain a more representative image of the influence the grouping method would have. All 5 scenarios were selected according to the FAA formulation. The results obtained can be seen in the following charts:

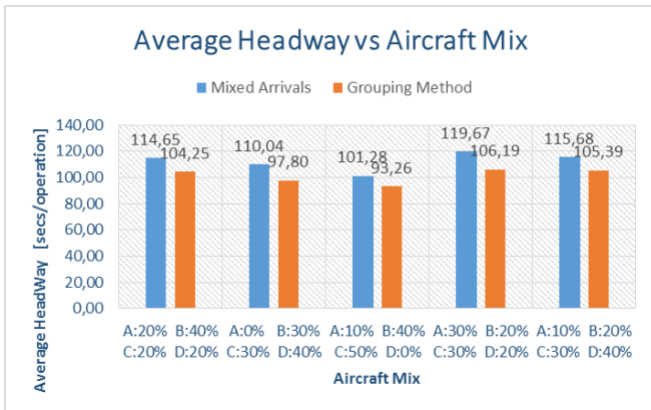


Figure 4 Average Headway vs Aircraft Mix

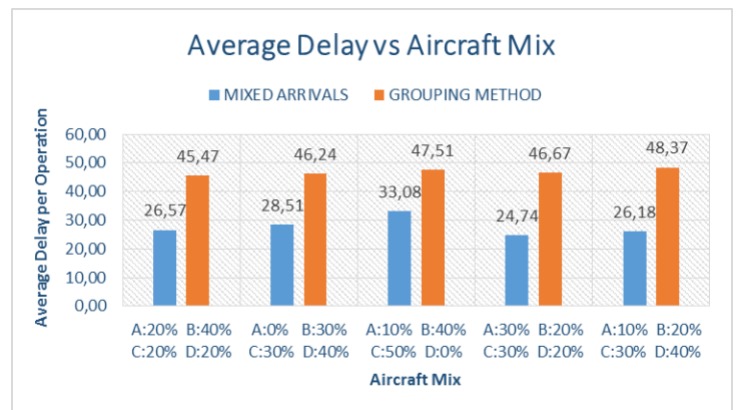


Figure 3 Average Delay vs Aircraft Mix

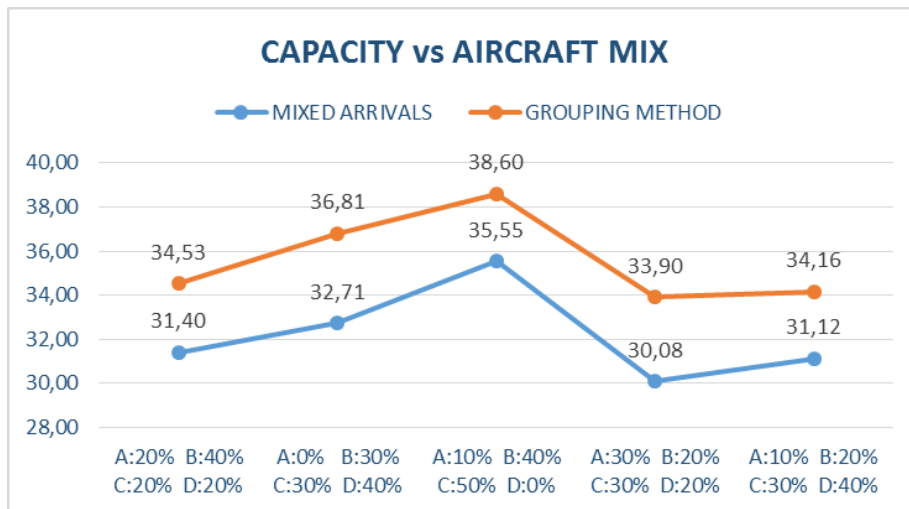


Figure 5 Capacity vs Aircraft Mix

In addition, the influence the cycle size has in the grouping method was analyzed:

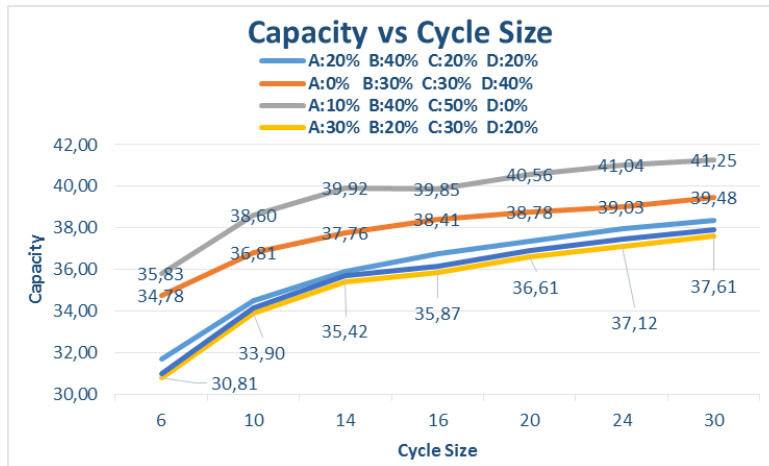


Figure 6 Capacity vs Cycle Size

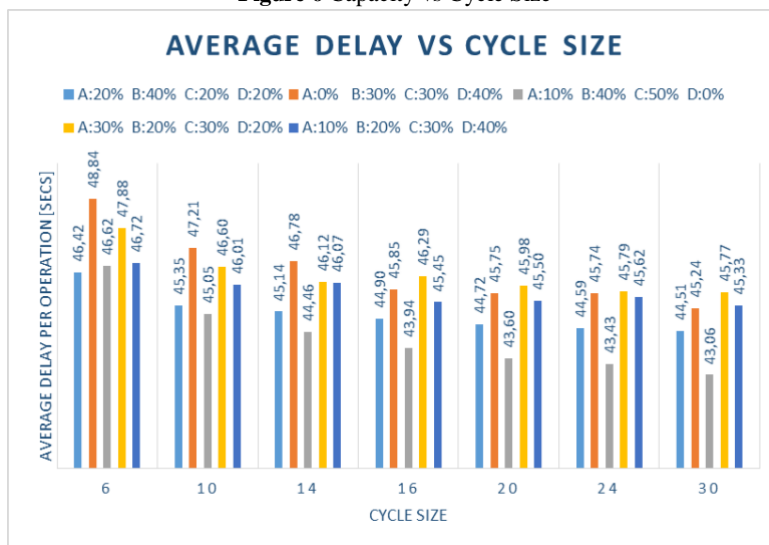


Figure 7 Average Delay vs Cycle Size



Figure 8 Average Delay Individual Scenario Analysis vs Cycle Size

Conclusions:

The aviation industry will have to face a continuous increase in demand that will require important upgrades in airports at all levels. After the results obtained in this paper, it can be concluded that the grouping method could be one solution for the upcoming congested periods. In all cases studied in this paper and solved with the program developed, the grouping method obtains better results in terms of airfield capacity. However, it has to be said that in non-congested periods the application of this technique will not make sense as it provides greater average delay than the FCFS.

As a final conclusion, the grouping method results are at first approach, good enough for taking it into consideration for further research on this field. It should be analyzed and optimized using software and technologies available at airports. In addition, it would be optimal to develop a program that allows air traffic controllers to dynamically switch between both methods whenever the FCFS cannot afford the demand levels.

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ABSTRACT

According to the FAA, Aviation and especially passenger flow has been consistently growing for the last 10 years and it is expected to continue with this growth (Federal Aviation Administration, 2019). Alongside this growth, airports and aviation resources are likely to reach its full operational potential in the next years making progress and development a priority. The ultimate goal of this paper is to study the viability of using a group method for landings in order to obtain a greater value of the airfield capacity. It specifically deals with a comparison between the actual method used in airports when they are experiencing take-offs & landings (FCFS), and a possible platoon-based method that could be adopted by the airports. In this paper, the formulation of the capacity & average delay for the grouping method has been developed and the sensitivity analysis completed shows that there is room for improvement in terms of capacity. The grouping method would increase the capacity in comparison to the (FCFS). However, it leads to a larger average delay meaning that there will be periods where it would be reasonable to adopt this technique when delay is not a concern and capacity is more important.

INTRODUCTION

Airfield or runway capacity is defined as the maximum sustainable throughput of aircraft operations, i.e. both arrivals and departures that can be achieved during a specified time interval (e.g. 1 hour) at a given airport with a specific runway layout, under different weather conditions, and at an acceptable level of delay. It indicates the average number of movements that can be performed on the runway system in 1 hour in the presence of continuous demand while meeting all the requirements imposed by the corresponding Aviation Administration (FAA in the USA) and air traffic management (ATM) system. The capacity of the airfield and especially of the runway typically determines the ultimate capacity of an airport.

There has been a great research during the past five decades on computing this airfield capacity as well as determining new methods to define and measure it. Air traffic demand is one important factor when determining the capacity as it determines whether an airport is congested or not at any time. An important variable in this relationship, is the mean departure/arrival rate which is defined as the safely permissible interoperation time for arrivals and departures.

According to a new report from the International Air Transport Association (IATA), passenger numbers are likely to surge in the next couple of decades. IATA expects 8.2 billion passengers to travel by air in 2037, a near doubling of today's 3.8 billion level. *Fig. 1* shows the passenger flow development of San Diego Airport from 1970 until 2018.

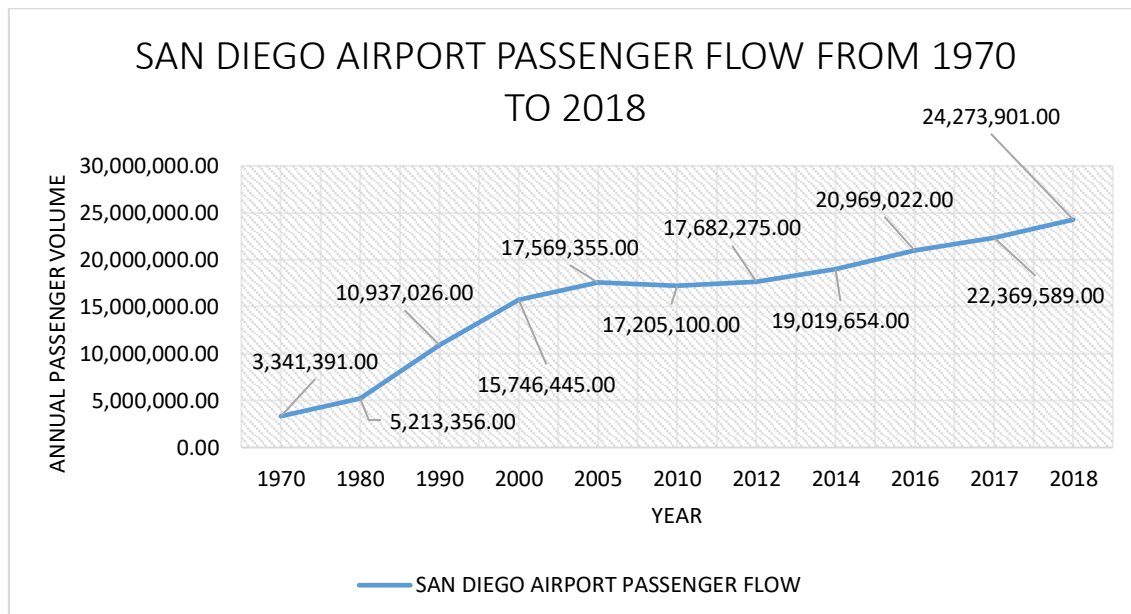


Figure 1 Passenger Flow Evolution

Data Source: FAA

This expected doubling in air travel is placing extra strain on airports that are already creaking at the seams. New challenges include improvements in airfield capacity technologies in order to be able to maintain the passengers flow in an efficient and cost-effective way, plus satisfying the rising security standards now required worldwide.

The huge growth in terms of passenger flow leading to an increase in airfield operations justifies a review of the methods used worldwide to keep the capacity of the airports as high as possible. Nowadays, the airports operate on a first-come, first serve (FCFS) basis where the aircraft land according to the order in which they have asked for permission. This method is probably the most effective and the best one for non-congested periods. However, at times when the airports are suffering from air traffic congestion (which will be very likely to happen at the growth rates we are currently experiencing) there is room for improvement in the FCFS, as we will discuss in this paper. The method that will be analyzed in this paper is based on grouping of aircraft.

The grouping method will divide the upcoming arrivals into cycles of platoons of the same aircraft class and approach speed in order to reduce the time between each. We will study the viability of this method from a basic case of an airport with one runway (e.g. San Diego Airport) and some reasonable assumptions. It will also be analyzed the possibility of using mixed-runways in order to incorporate take-offs between following landings in the cases they meet all safety requirements imposed by the Federal Aviation Administration (FAA).

Prior to start analyzing/studying the airfield capacity, it is necessary to define some of the basic knowledge regarding aircraft types and Landing/Departures procedures. The FAA (Federal Aviation Administration) divides all aircraft in three large groups according to their maximum certified take-off weight (MTOW):

Aircraft Class	Max. Certified T.O weight (lbs.)	Number of engines	Wake Turbulence Classification
A	12,500 or less	Single	SMALL (S)
B		Multi	
C	12,500-300,000	Multi	LARGE (L)
D	Over 300,000	Multi	HEAVY (H)

Table 1 Aircraft Class According to MTOW & Wake Turbulence Classification

Source: FAA

The FAA also identifies the Boeing 757 as an independent class because its MOTW is on the borderline between the Large and Heavy classes and it produces strong wake-vortex effects. For this study so far, we will assume this class negligible, as the number of Boeing 757 is too low compared to the other classes.

Another important classification when computing the capacity of an airfield is considering the approach speed of aircraft during landings. The following table from ICAO (International Civil Aviation Organization) sorts the aircraft according to their approach speed:

Aircraft Class	Approaching speed (KNOTS) V_{AT}	Maximum speeds for circling	Wake Turbulence Classification	Typical aircraft in this category
A	<91	100	Small	Small Single engine
B	91-120	135	Small	Small Multi engine
C	121-140	180	Large	Airline Jet
D	141-165	205	Heavy	Large Jet/Military Jet

Table 2 Aircraft Type & Corresponding Approaching Speed of Landings

Source: ICAO

Separation Requirements for Aircraft Operating to/from the same runway

One of the most important factors in determining runway capacity is the minimum longitudinal separation requirements for aircraft landing or departing from the same runway. These separation requirements are usually given in units of distance or time, and are determined by the wake turbulence produced by each aircraft class. The FAA provides the following specifications for these four cases:

Single-Runway IFR Separation Requirements in the U.S.

i. Arrival followed by Arrival (A-A)

Depending on the aircraft class, the following aircraft types must be separated by at least the distance (in Nautical Miles) indicated below:

Leading Aircraft	Nautical Miles	Trailing Aircraft		
		Heavy	Large	Small
	Heavy	4	5	5/6*
	Large	2.5 (or 3)	2.5 (or 3)	3/4*
	Small	2.5 (or 3)	2.5 (or 3)	2.5 (or 3)

Table 3 Arrival followed by Arrival Separation Requirements

Source: FAA

*Distances required at the time when the leading aircraft is at the threshold of the runway.

The trailing aircraft cannot touchdown on the runway until the leading aircraft is clear of the runway.

ii. Arrival followed by Departure (A-D)

Clearance for take-off run of the trailing aircraft is granted after the preceding landing is clear of the runway.

iii. Departure followed by Departure (D-D*)

Clearances for take-off runs of successive aircraft must be separated by at least the amount of time (in seconds) indicated below:

Leading Aircraft		Trailing Aircraft		
		H	L	S
	H	90	120	120
	L	60	60	60
	S	45	45	45

Table 4 Departure followed by Departure Safety Requirements

Source: FAA

*These times shown are approximations and somewhat conservative estimates of the time separations that result in practice. There are more complicated sets of rules that must be satisfied, which will be discussed below.

iv. Departure followed by Arrival (D-A)

The trailing arrival (regardless of its size or class) must be at least 2 Nautical Miles away from the runway at the time when the departing aircraft begins its takeoff run. The departing aircraft must also be clear of the runway before the trailing aircraft touches down on it.

METHODOLOGY

➤ Airfield Capacity: Mixed Arrivals vs Grouping Method

We will use a landing intervals-model based in order to estimate runway capacity. This model accounts for the following factors:

- I. Length of common approach path (γ).
- II. Approaching speed of aircraft
- III. Minimum separation requirements.

We will first compute this capacity for a random order of arrival (mixed) and then, for a cycle based method so we can analyze the difference. We will also study how much impact this grouping method would have in terms of delay when switching the number of planes in each platoon.

This model assumes error-free approaches, which means that controllers are able to deliver aircraft to the entry gate exactly at scheduled times and pilots are able to maintain the required separations, aircraft speeds, and alignments with the runway for landing accurately. Therefore, we need to define two different situations for these landings, (a) the overtaking case, in which the trailing aircraft has a speed equal or greater than the lead aircraft, and (b) the opening case, in which the approaching speed of the leading aircraft is greater than the trailing one. The following time-space diagrams show both situations for consecutive landings in one runway. (Norman J. Ashford, 2011)

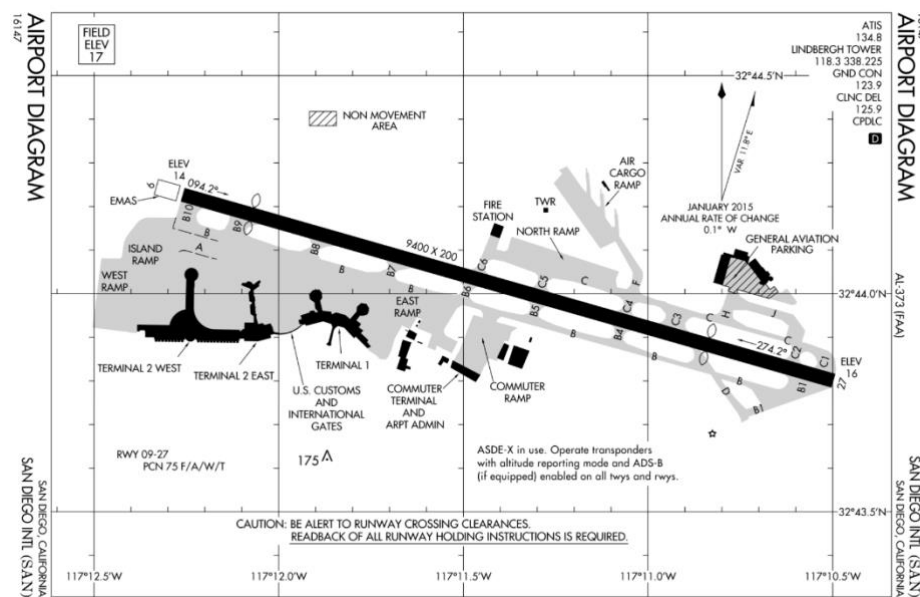


Figure 2 San Diego Airport Layout.

Source: FAA

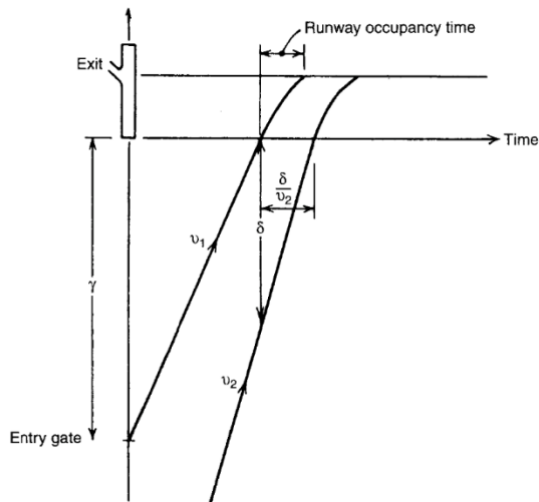


Figure 4 (a) Overtaking Case

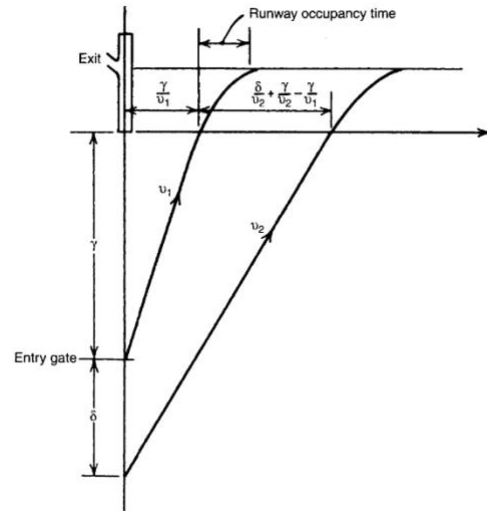


Figure 3 (b) Opening Case

The variables for this model would be:

Variable	Definition	Units
V_i	Speed of Aircraft i	$\frac{NM}{hour}$ (KNOTS)
γ	Length of Common Approach Path	NM
δ_{ij}	Safety Separation between speed class i followed by speed class j	NM
$h(i,j)$	Headway between leading aircraft i followed by aircraft j	Seconds
P_i	Aircraft Mix	%
h	Average Headway	Seconds
C	Capacity	$\frac{Operations}{Hour}$
N_i	Number of planes of speed class i	# Planes
ROT_i	Runway Occupancy Time for Aircraft type i	Seconds
Q_i	Platoon Size of Aircraft type i	$\frac{Planes}{Platoon}$
T	Number of Cycles	# Cycles
Z	Number of Platoons per Cycle	Platoons
D_i	Platoon duration of Aircraft type i	Seconds
O	Operations per Cycle	Operations

Table 5 Variables for the model

1) **Probabilities for each aircraft speed class:**

$$P_i = \frac{N_i}{\sum_{j=1}^n N_j} \text{ [Aircraft Mix]}$$

2) **Minimum Headway between landings:**

The calculation for this section varies depending on the overtaking or opening case:

- **Overtaking Case ($V_j \geq V_i$)**

$$h_{ij}(\text{Overtaking}) = \frac{\delta_{ij}}{V_j} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} \text{ [secs]} \quad \text{For } \begin{cases} i = \text{Leading Aircraft type} \\ j = \text{Trailing Aircraft type} \end{cases}$$

- **Opening Case ($V_j < V_i$)**

$$h_{ij}(\text{Opening}) = \left(\frac{\delta_{ij}}{V_j} + \gamma \cdot \left(\frac{1}{V_j} - \frac{1}{V_i} \right) \right) \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} \text{ [secs]} \quad \text{for } \begin{cases} i = \text{Leading Aircraft type} \\ j = \text{Trailing Aircraft type} \end{cases}$$

3) **Minimum Headway Matrix:**

Basic Case (Only accounts 2 type of Aircrafts (e.g. Small & Large)):

Trailing Aircraft (j)	Leading Aircraft (i)			Probabilities (P _j)
		Small (1)	Large (2)	
	Small (1)	h _{SS}	h _{LS}	P _{small}
Large (2)	h _{SL}	h _{LL}	P _{large}	
Probabilities (P _i)		P _{small}	P _{large}	

Table 6 Headway Matrix for Small & Large Planes

General Case with all Aircraft types taken into account:

Trailing Aircraft (j)	Leading Aircraft (i)				Probabilities (P _j)
	A	B	C	D	
A	h _{AA}	h _{BA}	h _{CA}	h _{DA}	P _A
B	h _{AB}	h _{BB}	h _{CB}	h _{DB}	P _B
C	h _{AC}	h _{BC}	h _{CC}	h _{DC}	P _C
D	h _{AD}	h _{BD}	h _{CD}	h _{DD}	P _D
Probabilities (P _i)		P _A	P _B	P _C	P _D

Table 7 Headway Matrix for all aircraft types

4) **Total Headway:**

$$h = \sum_{i=1}^{i=n} \sum_{j=1}^{j=n} P_i \cdot h_{ij} \cdot P_j \text{ [Seconds]}$$

5) **Capacity:**

$$h = \frac{1}{\text{Avg Headway}} = \frac{1}{\sum_{i=1}^{i=n} \sum_{j=1}^{j=n} P_i \cdot m_{ij} \cdot P_j} \left[\frac{\text{Arrival}}{\text{Seconds}} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} \right] \rightarrow \left[\frac{\text{Arrivals}}{\text{Hour}} \right]$$

The formulation above would allow us to estimate the capacity for a mixed sequence of arrivals without using the grouping method. As long as we want to compare the results obtained with the grouping method, we need to formulate the capacity for the grouping method as follows:

1) **Cycle Dimension Definition:**

$$1 \text{ Cycle} = 1 \text{ Platoon Planes type } (i) + 1 \text{ Platoon Planes type } (i + 1) + \dots + 1 \text{ Platoon Planes type } (i + n - 1)$$

2) **Platoon Probability:**

$$P_{\text{platoon}(i)} = \frac{Z_i}{\sum_{i=1}^n Z_i} \text{ where } \{Z_i = \text{Platoons of aircraft } i \text{ per cycle}\}$$

3) **Headway Matrix:**

Trailing Aircraft (j)	Leading Aircraft (i)				Probabilities (P _j)
	A	B	C	D	
A	h _{AA}	h _{BA}	h _{CA}	h _{DA}	P _{platoonA}
B	h _{AB}	h _{BB}	h _{CB}	h _{DB}	P _{platoonB}
C	h _{AC}	h _{BC}	h _{CC}	h _{DC}	P _{platoonC}
D	h _{AD}	h _{BD}	h _{CD}	h _{DD}	P _{platoonD}
Probabilities (P _i)	P _{platoon A}	P _{platoon B}	P _{platoon C}	P _{platoon D}	

Table 8 Headway Matrix for Grouping Method

4) **Average headway between arrivals within the cycle:**

$$h_{\text{cycle}} = \frac{D_A + D_B + D_C + D_D + \sum Z_i \cdot D_{\text{platoon shift}}}{\# \text{ of Planes per Cycle}}$$

where $\{\sum Z_i = \text{Total number of platoons shifts within a cycle.}\}$

We compute the different headways which are in equation above as follows:

- $D_{duration\ platoon\ A} = (Q_A - 1) \cdot (h_{aa})$
- $D_{platoon\ B} = (Q_B - 1) \cdot (h_{bb})$
- $D_{platoon\ C} = (Q_C - 1) \cdot (h_{cc})$
- $D_{platoon\ D} = (Q_D - 1) \cdot (h_{dd})$

where $\{Q_i = \text{Number of planes within platoon } i\}$

- $D_{platoon\ shift} = \sum_{i=1}^n \sum_{j=1}^n P_{platoon\ i} \cdot h_{ij} \cdot P_{platoon\ j} \left[\frac{Secs}{platoon-shift} \right]$

5) Capacity for the grouping method:

$$C = \frac{1}{h_{cycle}} \cdot \frac{3600\ sec}{1\ hour} = \left[\frac{Arrivals}{hour} \right]$$

Take-Offs Between Landings Formulation

The ultimate goal of this paper is to optimize the runway capacity so the airports can hold as many operations/hour as possible. Therefore, it is really interesting to study the viability of integrating Take offs in the gap between consecutive landings. In this case the runway will be running both operations (take-offs & landings) at the same time and it would be known as a mixed operations runway. For this to be possible, it is necessary to meet the requirements explained above for Departures following landings (2 NM is the minimum required distance for the following arrivals).

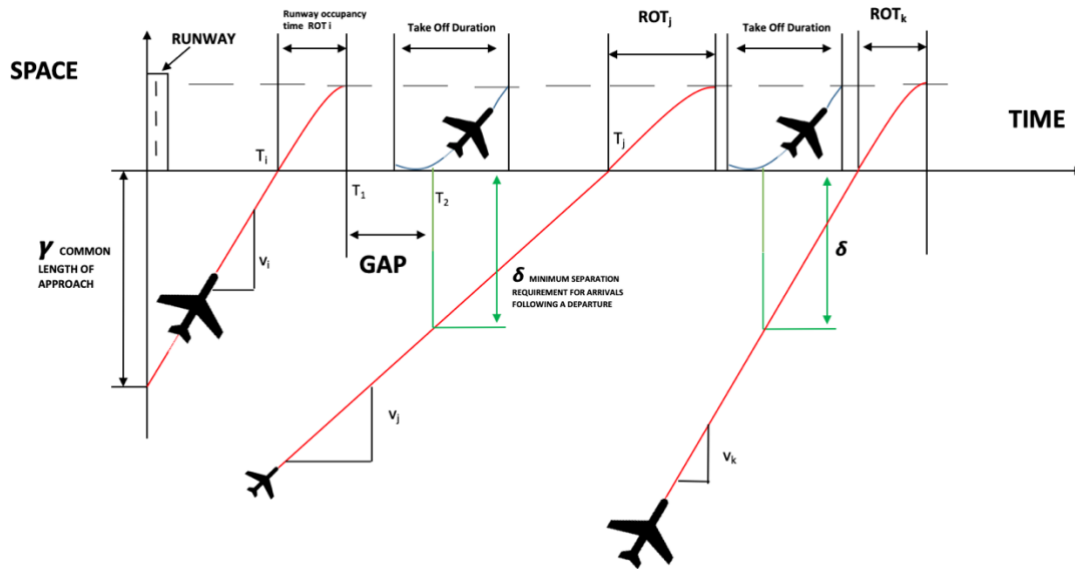


Figure 5 Takeoffs between landings Time-Space Diagrams

As Figure 5 shows, there is room for a plane to take-off to when:

$$T2 - T1 > 0;$$

$$T1 = Ti + ROT_i;$$

$$T2 = Tj - \frac{\delta}{v_j};$$

Where:

$$\left\{ \begin{array}{l} T1 = \text{Time when the precedent arrival exits the runway} \\ T2 = \text{Time when the departure begins its takeoff run} \\ \text{taking into account the safety margin for the upcoming arrival} \end{array} \right.$$

➤ **Take-Offs Between Landings Optimization**

As stated above, there must exist a gap between two consecutive landings in order to insert a take-off between them. However, there are some border cases where the gap needs only a few more seconds in order to allow the take-off to take place. In this light, sometimes it is more beneficial for the airfield capacity to delay the incoming arrival those seconds and let the ATM use the runway, because this would mean an increase in the number of operations the airport could perform with an insignificant or very low, time cost. The formulation for this analysis would be the following:

VARIABLE	DESCRIPTION	UNITS
h_{CYCLE}	Headway for the grouping method	Secs
T	Time necessary to perform a take-off	Secs
A_{CYCLE}	Airfield Capacity for the grouping method	Operations/hour
q	Number of Cycles	Cycles per hour
N	Number of takeoffs that could be performed within a cycle	Operations/cycle

Table 9 Variables for Take-Offs Optimization

As we know from the formulation of previous sections, the airfield capacity is computed as the inverse of the headway. Therefore, a delay should be applied to the upcoming arrival when the following equation is met:

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

Therefore, an analysis of these possible situations will be developed with the results obtained for the gaps in both scenarios.

➤ **Delay for Mixed Arrivals Formulation**

A simple runway system can be described by mathematical models or formulas of queueing theory. Arrivals can be satisfactorily described by the Poisson probability distribution. Queueing theory addresses congestion and its causes, and explores the relationships between demand on a service system and congestion in the system manifested by delays suffered by the system users. However, this equations serve us to understand the delay-capacity relationships, they may not provide accurate estimates of average delay, except for simple situations. Assuming Poisson arrivals and constant service times, the Pollaczek-Khinchin formula was derived for average landing delay (Norman J. Ashford, 2011):

$$W = \frac{\rho}{2 \cdot \mu(1 - \rho)} = \frac{\rho(1 + Cb^2)}{2\mu(1 - \rho)}$$

In order to know what information is needed to compute the average delay for the mixed/random arrivals method, the following variables are defined:

Variable	Description	Units
W	Average Delay	Hours per Arrival
ρ	Load factor	Dimensionless
μ	Mean Runway service time	Seconds per operation
λ	Arrival Rate (Capacity)	Arrivals/Hour
σ	Standard deviation of Mean service time	Seconds per operation
Cb	Coefficient of Variation	Dimensionless
ROTi	Runway occupancy time for Aircraft Class i	Seconds

Table 10 Variables for Average Delay (Pollaczek-Khinchin formula)

- **Mean Runway Service Time & Standard Deviation of Mean Service Time:**

$$\mu = \sum_{i=A}^N \frac{ROT_i}{N} \text{ [Seconds/operation]}; \quad \sigma = \sqrt{\frac{\sum_{i=A}^N (ROT_i - \mu)^2}{N}}$$

- **Coefficient of Variation**

$$Cb = \frac{\sigma}{\mu}$$

- **Load Factor:**

$$\rho_{mixed} = \frac{\lambda_{mixed}}{\mu} = \frac{\lambda_{mixed} \cdot \frac{Arrivals}{Hour}}{\frac{1}{\mu \cdot \frac{Seconds}{Arrival}} \cdot \frac{3600secs}{Hour}}$$

$$\rho_{cycle} = \frac{\lambda_{cycle}}{\mu} = \frac{\lambda_{cycle} \cdot \frac{Arrivals}{Hour}}{\frac{1}{\mu \cdot \frac{Seconds}{Arrival}} \cdot \frac{3600secs}{Hour}}$$

- **Average Delay per Operation:**

$$W_{Mixed} = \frac{\rho_{mixed}(1 + Cb^2)}{2\mu(1 - \rho)}$$

$$W_{Cycle} = \frac{\rho_{cycle}(1 + Cb^2)}{2\mu(1 - \rho)}$$

➤ **Delay for the Grouping Method**

For the grouping method delay analysis, the variables would be:

Variable	Description	Units
D_i	Duration of platoon i per cycle	Seconds
T	Duration of the cycle	Seconds
A_i	Aircraft mix of aircraft type i	Dimensionless
$D_{\text{platoon shift}}$	Average time duration for platoon shifts	Seconds
N	Planes per Cycle	Operations
W	Average Delay	Seconds Per Operation

Table 11 Variables Average Delay for the Grouping Method

To estimate this average delay, we will assume a total waiting time of half of the duration of its platoon in the case the plane arrives at the same time its platoon has obtained permission to begin landing. Otherwise, if the plane arrives when a different group is landing, it will have to wait the duration of all the others platoons plus half of its own. This a very simple and conservative way of calculating the average delay that will give us a reasonable approach and comparison to the mixed one. Therefore, the formulation for this first approach would be the following:

- **Platoon probability between each cycle:**

$$P_i = \frac{D_i}{\sum_i^n D_i} = \frac{D_i}{T}$$

- **Average Delay for two Groups (Small [Class A] & Large[Class C])**

$$W = A_{small} \cdot \left(P_{small} \cdot \frac{1}{2} \cdot D_{small} + P_{large} \cdot \left(D_{large} + h_{shift} + \frac{1}{2} D_{small} \right) \right) + A_{large} \cdot \left(P_{large} \cdot \frac{1}{2} \cdot D_{large} + P_{small} \cdot \left(D_{small} + h_{shift} + \frac{1}{2} D_{large} \right) \right)$$

$$D_{shift} = A_{small} \cdot h_{small-large} + A_{large} \cdot h_{large-small}$$

➤ **Average delay for all aircrafts groups**

The shift headway will be computed as mean of the all headway shifts as we will assume that the platoon order inside a cycle is not known. Therefore, the shift headway would be the following:

$$D_{shift} = \sum_{i=A}^D A_i \cdot \sum_{j=A}^D \frac{h_{ij}}{N-1} \quad \text{for all} \quad i \neq j$$

Cycle Order: Platoon A – Platoon B – Platoon C – Platoon D

Average delay for Aircraft type A:

$$W_A = A_A \cdot \left(P_A \cdot \frac{1}{2} \cdot D_A + P_B \cdot \left(D_B + D_C + D_D + 3 \cdot h_{shift} + \frac{1}{2} \cdot D_A \right) + P_C \cdot \left(D_C + D_D + 2 \cdot h_{shift} + \frac{1}{2} \cdot D_A \right) + P_D \cdot \left(D_D + h_{shift} + \frac{1}{2} \cdot D_A \right) \right)$$

Average delay for Aircraft type B:

$$W_B = A_B \cdot \left(P_B \cdot \frac{1}{2} \cdot D_B + P_C \cdot \left(D_C + D_D + D_A + 3 \cdot h_{shift} + \frac{1}{2} \cdot D_B \right) + P_D \cdot \left(D_D + D_A + 2 \cdot h_{shift} + \frac{1}{2} \cdot D_B \right) + P_A \cdot \left(D_A + h_{shift} + \frac{1}{2} \cdot D_B \right) \right)$$

Average delay for Aircraft type C:

$$W_C = A_C \cdot \left(P_C \cdot \frac{1}{2} \cdot D_C + P_D \cdot \left(D_D + D_A + D_B + 3 \cdot h_{shift} + \frac{1}{2} \cdot D_C \right) + P_A \cdot \left(D_A + D_B + 2 \cdot h_{shift} + \frac{1}{2} \cdot D_C \right) + P_B \cdot \left(D_B + h_{shift} + \frac{1}{2} \cdot D_C \right) \right)$$

Average delay for Aircraft type D:

$$W_D = A_D \cdot \left(P_D \cdot \frac{1}{2} \cdot D_D + P_A \cdot \left(D_A + D_B + D_C + 3 \cdot h_{shift} + \frac{1}{2} \cdot D_D \right) + P_B \cdot \left(D_B + D_C + 2 \cdot h_{shift} + \frac{1}{2} \cdot D_D \right) + P_C \cdot \left(D_C + h_{shift} + \frac{1}{2} \cdot D_D \right) \right)$$

Average Delay for any plane in the cycle when the grouping method is being used:

$$W_{cycle} = W_A + W_B + W_C + W_D$$

RESULTS

➤ Basic Case – 1 Runway & 2 Aircraft Types

Ns (Small Planes)	N _L (Large Planes)	P Aircraft Mix Small (A)	P _L Aircraft Mix Large (C)	V _s Velocity of Small	V _L Velocity of Large	γ length of common approach	Platoons per Cycle	Cycle Size (Planes per Cycle)
4	6	40%	60%	91	121	6	2	10

Table 12 Basic Case Parameters

Mixed Method Time-Space Diagram:

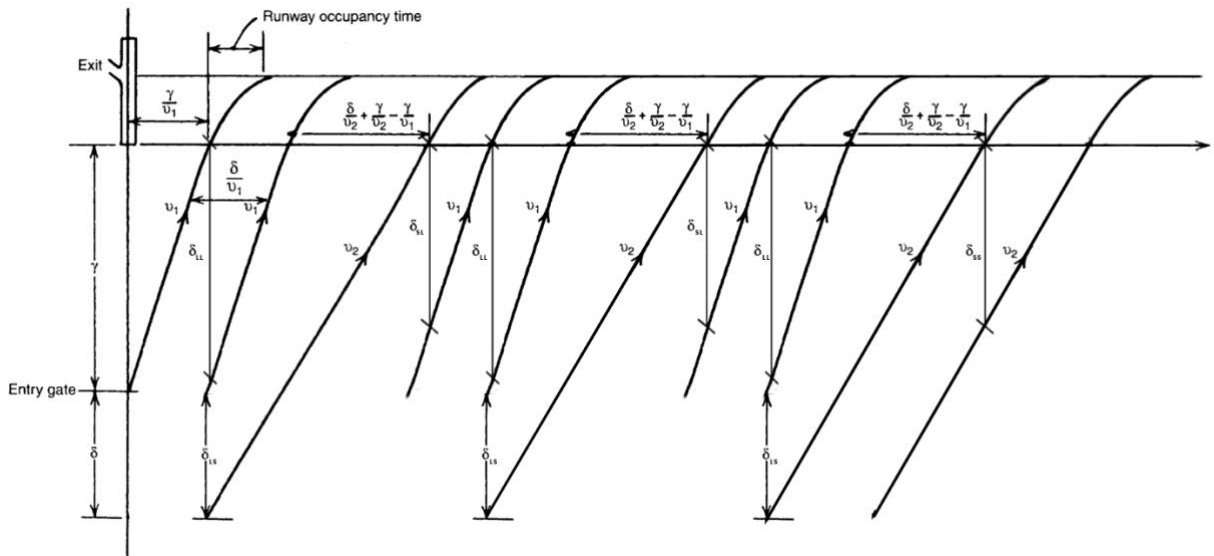


Figure 6 Time Space Diagram for Random Order Arrivals

Grouping Method Time-Space Diagram:

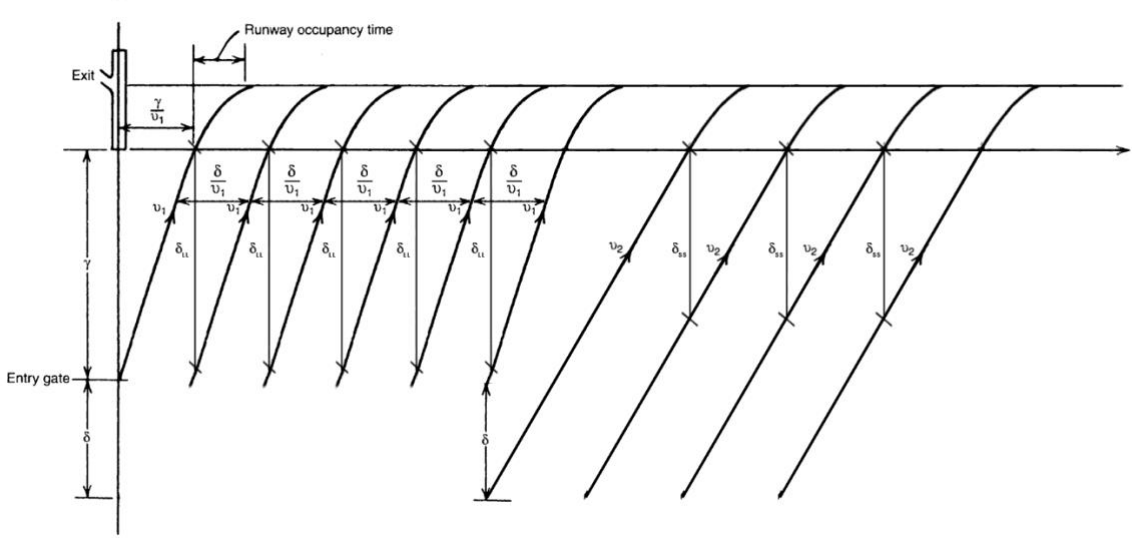


Figure 7 Time Space Diagram for the grouping method Arrivals

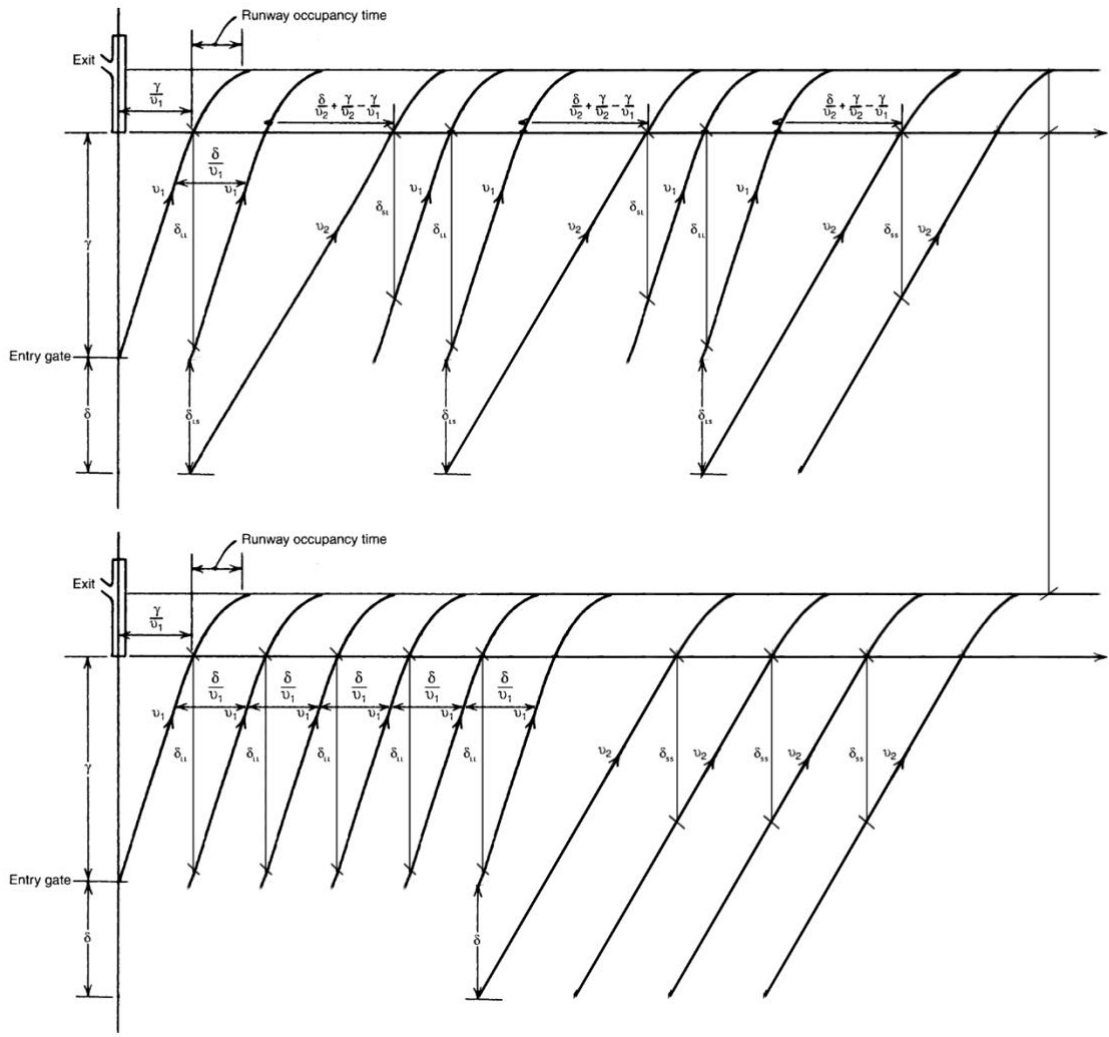


Figure 8 Time Space Diagrams Comparison

Headway Matrix for Mixed Arrivals:

Trailing Aircraft (j)	Leading Aircraft (i)		Probabilities (P _j)
	Small (A)	Large (C)	
Small (A)	98.91	217.092	0.4
Large (C)	74.38	89.25	0.6
Probabilities (P _i)	0.4	0.6	

Table 13 Basic Case Headway Matrix Mixed Arrivals

Headway Matrix for Grouped Arrivals:

Trailing Aircraft (j)	Leading Aircraft (i)			Platoon Probability
		Small (Planes type A)	Large (Planes type C)	
	Small (A)	98.91	217.092	0.5
	Large (C)	74.38	89.25	0.5
Platoon Probability		0.5	0.5	

Table 14 Basic Case Headway Matrix Grouping Method

Once the formulation explained above is applied for this specific problem we obtain the following result, that shows a clear increase of the airfield capacity when the hypothetical airport operates with a grouping-method.

METHOD	AVG HEADWAY	CAPACITY
MIXED ARRIVALS	117.91 secs	30.5 $\frac{\text{operations}}{\text{hour}}$
GROUPED ARRIVALS	88.87 secs	40.51 $\frac{\text{operations}}{\text{hour}}$

Table 15 Summary Results Basic Case

Furthermore, a sensitivity analysis was carried out comparing how much the capacity would change when the airport expects aircraft mixes different from (40% A & 60% C). The chart below clearly reveals an increase of the capacity when the number of planes of type C is greater than the number of A planes.

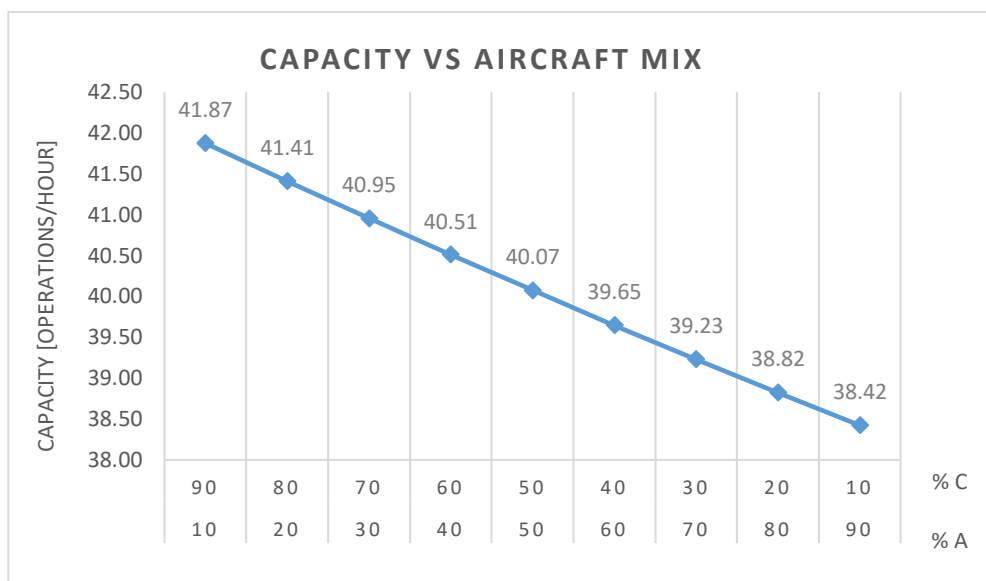


Figure 9 Capacity versus Aircraft Mix Comparison

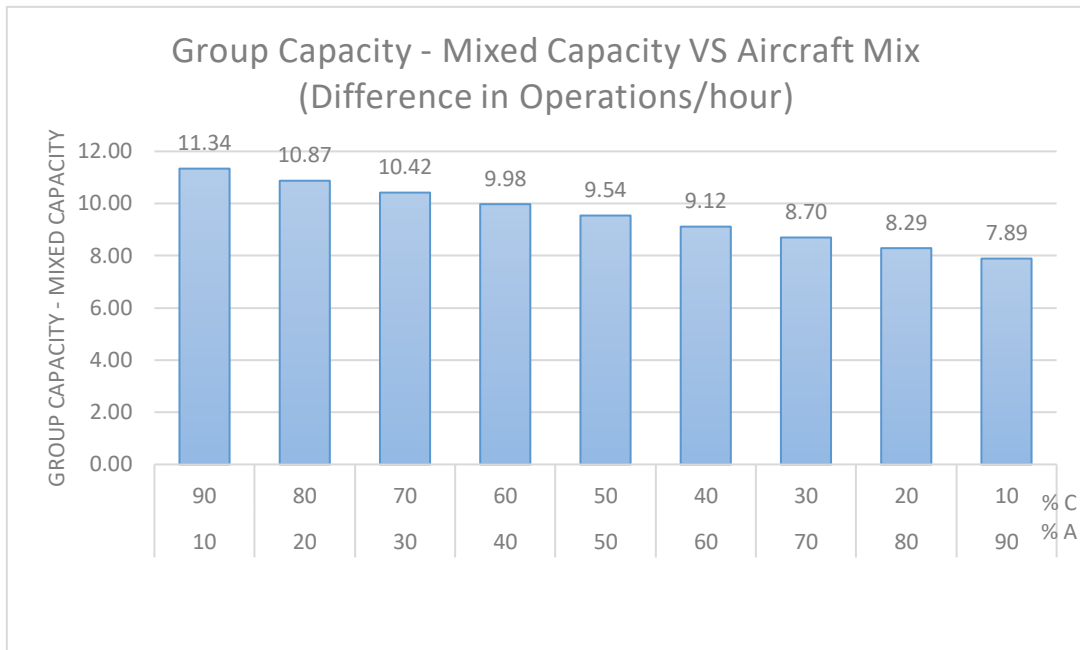


Figure 10 Difference in Airfield Capacity between Grouping Method and Random order for different mixes

➤ **2nd Scenario 1 Runway & 4 Aircraft Types**

The second scenario we will be studying is the same one-runway airport but in this case any type of aircraft could be asking permission for landing. Therefore, we will have one runway and four aircraft types. The data used to simulate this scenario is the following:

AIRCRAFT TYPE	APPROACHING SPEED	AIRCRAFT MIX	PLANES PER PLATOON
A	90 KNOTS	20%	2
B	110 KNOTS	40%	4
C	130 KNOTS	20%	2
D	150 KNOTS	20%	2
TOTAL PLANES PER CYCLE			10

Table 16 2nd Scenario Parameters

The results obtained for this simulation still reveal an improvement in airfield capacity when the airport is using a grouping method. This means that there could be room for improvement in this area although we are making important assumptions.

METHOD	AVG HEADWAY	CAPACITY
MIXED ARRIVALS	119.85 secs	30.04 $\frac{\text{operations}}{\text{hour}}$
GROUPED ARRIVALS	104,5 secs	34,53 $\frac{\text{operations}}{\text{hour}}$

Table 17 2nd Scenario Results

The above calculations accounts for a cycle size of 10 planes. It is interesting to analyze the effects the cycle size would have on the final airfield capacity. We can see this in Fig. 9:

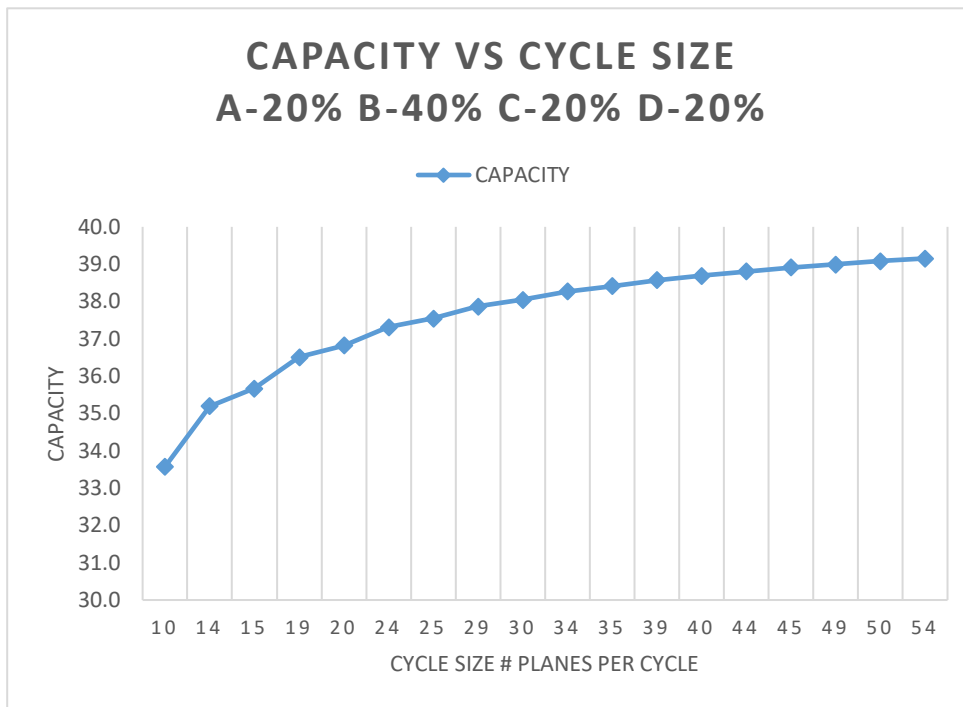


Figure 11 Capacity versus Cycle Size for a determined Aircraft Mix

From Fig. 11 we can conclude that the cycle size does affect the airfield capacity but less than switching from the FCFS method to the grouping method. As we can see, the capacity difference between the smallest cycle size (10 planes) with the biggest cycle size (54 planes) is only 1.8 Arrivals per hour more.

In addition, it is interesting to investigate how much the capacity would change when airports experience different aircraft mixes than the ones used for the mathematical calculation. Therefore, for the given typical speeds of each aircraft type the fluctuation on capacity due to the aircraft mix is the following:

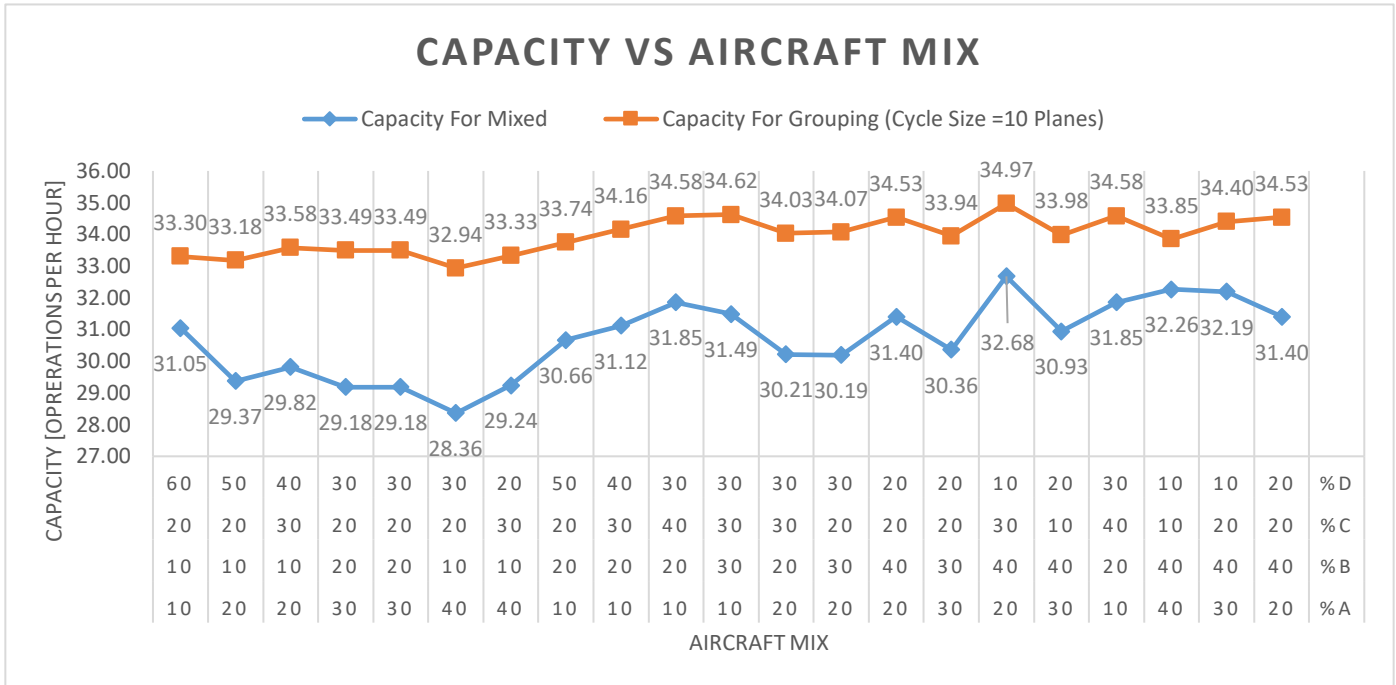


Figure 12 Capacity versus Aircraft Mix with Four Aircraft Types

➤ **Gaps for the Basic Case**

Velocity of Small	Velocity of Large	Safety Margin δ (Specified by the FAA)	ROTs for Small Arrivals	ROT _L for Large Arrivals	H _{ss} Headway for small-large	H _{ll} Headway for large-large	H _{LS} Headway for large-small	H _{SL} Headway Small-Large
91 Knots	121 Knots	2 NM	40 secs	45 secs	98.9 secs	89.26 sec	217.09 sec	74.38secs

Table 18 Parameters Gaps for the Basic Case

1. **TAKEOFF BETWEEN SMALL-SMALL ARRIVAL:**

$$T1 = Ti + ROTs = 0 + 40 = 40secs$$

$$T2 = H_{ss} - \frac{\delta}{V_s} = 98.9 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 19.8 secs$$

Gap Exists if $T2 - T1 > 0$ $Gap = T2 - T1 = 19.8 - 40 = -20.2secs$

→ NO TAKE OFF IS POSSIBLE

2. **TAKEOFF BETWEEN SMALL-LARGE ARRIVAL:**

$$T1 = Ti + ROTs = 0 + 40 = 40secs$$

$$T2 = Hsl - \frac{\delta}{Vl} = 74.38 - \frac{2}{121} \cdot \frac{3600secs}{1Hour} = 14.876 \text{ secs}$$

Gap Exists if $T2 - T1 > 0$ $Gap = T2 - T1 = 14.876 - 40 = -25.12secs$

→ NO TAKE OFF IS POSSIBLE

3. TAKEOFF BETWEEN LARGE-LARGE ARRIVAL:

$$T1 = Ti + ROTl = 0 + 45 = 45secs$$

$$T2 = Hll - \frac{\delta}{Vl} = 89.26 - \frac{2}{121} \cdot \frac{3600secs}{1Hour} = 29.76 \text{ secs}$$

Gap Exists if $T2 - T1 > 0$ $Gap = T2 - T1 = 29.76 - 45 = -10.24secs$

→ NO TAKE OFF IS POSSIBLE

4. TAKEOFF BETWEEN LARGE-SMALL ARRIVAL:

$$T1 = Ti + ROTl = 0 + 45 = 45secs$$

$$T2 = Hls - \frac{\delta}{Vs} = 217.09 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 137.97secs$$

Gap Exists if $T2 - T1 > 0$ $Gap = T2 - T1 = 137.97 - 45 = 92.97secs$

→ TAKE OFF IS POSSIBLE

➤ **Gaps for 1 Runway & 4 types of Aircraft:**

The formulation would be the same as the above calculations with the difference that in these case we have 16 possible Gaps:

Aircraft Type	Velocity (KNOTS)	ROTi	Safety Margin δ
A	91	40	2
B	110	43	2
C	130	48	2
D	150	53	2

LEADING AIRCRAFT					
TRAILING AIRCRAFT	HEADWAY MATRIX	A	B	C	D
	A	98,90	139,90	229,45	310,95
	B	81,82	81,82	161,12	232,36
	C	69,23	69,23	83,08	160,62
	D	60,00	60,00	72,00	96,00

Table 19 Parameters & Headway Matrix for 2nd Scenario Gaps Analysis

1. TAKEOFF BETWEEN A - A ARRIVAL:

$$T1 = Ti + ROTa = 0 + 40 = 40secs$$

$$T2 = HAA - \frac{\delta}{Va} = 98.9 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 19.8 \text{ secs}$$

Gap Exists if $T2 - T1 > 0$ $Gap = T2 - T1 = 19.8 - 40 = -20.2secs$

→ NO TAKE OFF IS POSSIBLE

2. TAKEOFF BETWEEN A – B ARRIVAL:

$$T1 = Ti + ROTa = 0 + 40 = 40secs$$

$$T2 = H_{AB} - \frac{\delta}{Vb} = 81.82 - \frac{2}{110} \cdot \frac{3600secs}{1Hour} = 16.36 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 16.36 - 40 = -23.64secs$$

→ NO TAKE OFF IS POSSIBLE

3. TAKEOFF BETWEEN A - C ARRIVAL:

$$T1 = Ti + ROTa = 0 + 40 = 40secs$$

$$T2 = H_{AC} - \frac{\delta}{Vc} = 69.23 - \frac{2}{130} \cdot \frac{3600secs}{1Hour} = 13.85 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 13.85 - 40 = -26.15secs$$

→ NO TAKE OFF IS POSSIBLE

4. TAKEOFF BETWEEN A - D ARRIVAL:

$$T1 = Ti + ROTa = 0 + 40 = 40secs$$

$$T2 = H_{AC} - \frac{\delta}{Vd} = 60 - \frac{2}{150} \cdot \frac{3600secs}{1Hour} = 12 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 12 - 40 = -28 secs$$

→ NO TAKE OFF IS POSSIBLE

5. TAKEOFF BETWEEN B - B ARRIVAL:

$$T1 = Ti + ROTb = 0 + 43 = 43secs$$

$$T2 = H_{BB} - \frac{\delta}{Vb} = 81.82 - \frac{2}{110} \cdot \frac{3600secs}{1Hour} = 16.36 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 16.36 - 43 = -26.63secs$$

→ NO TAKE OFF IS POSSIBLE

6. TAKEOFF BETWEEN B - A ARRIVAL:

$$T1 = Ti + ROTb = 0 + 43 = 43secs$$

$$T2 = H_{BA} - \frac{\delta}{Va} = 139.9 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 60.78 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 60.78 - 43 = 17.78secs$$

→ TAKE OFF IS POSSIBLE

7. TAKEOFF BETWEEN B - C ARRIVAL:

$$T1 = Ti + ROTb = 0 + 43 = 43secs$$

$$T2 = H_{BC} - \frac{\delta}{Vc} = 69.23 - \frac{2}{130} \cdot \frac{3600secs}{1Hour} = 13.85 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 13.85 - 43 = -26.15secs$$

→ NO TAKE OFF IS POSSIBLE

8. TAKEOFF BETWEEN B - D ARRIVAL:

$$T1 = Ti + ROTb = 0 + 43 = 43secs$$

$$T2 = H_{AC} - \frac{\delta}{Vd} = 60 - \frac{2}{150} \cdot \frac{3600secs}{1Hour} = 12 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 12 - 43 = -31secs$$

→ NO TAKE OFF IS POSSIBLE

9. TAKEOFF BETWEEN C - A ARRIVAL:

$$T1 = Ti + ROTc = 0 + 48 = 48secs$$

$$T2 = H_{CA} - \frac{\delta}{Va} = 229.45 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 150.33 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 150.33 - 48 = 102.33 secs$$

→ TAKE OFF IS POSSIBLE

10. TAKEOFF BETWEEN C - B ARRIVAL:

$$T1 = Ti + ROTc = 0 + 48 = 48secs$$

$$T2 = H_{CB} - \frac{\delta}{Vb} = 161.12 - \frac{2}{110} \cdot \frac{3600secs}{1Hour} = 95.66 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 95.66 - 48 = 47.66 secs$$

→ TAKE OFF IS POSSIBLE

11. TAKEOFF BETWEEN C - C ARRIVAL:

$$T1 = Ti + ROTc = 0 + 48 = 48secs$$

$$T2 = H_{CC} - \frac{\delta}{Vc} = 83.08 - \frac{2}{130} \cdot \frac{3600secs}{1Hour} = 27.69 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 27.69 - 48 = -20.31 secs$$

→ NO TAKE OFF IS POSSIBLE

12. TAKEOFF BETWEEN C - D ARRIVAL:

$$T1 = Ti + ROTc = 0 + 48 = 48secs$$

$$T2 = H_{CD} - \frac{\delta}{Vd} = 72 - \frac{2}{150} \cdot \frac{3600secs}{1Hour} = 24 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 24 - 48 = -24 secs$$

→ NO TAKE OFF IS POSSIBLE

13. TAKEOFF BETWEEN D - A ARRIVAL:

$$T1 = Ti + ROTd = 0 + 53 = 48secs$$

$$T2 = H_{DA} - \frac{\delta}{Vd} = 310.95 - \frac{2}{91} \cdot \frac{3600secs}{1Hour} = 231.83 secs$$

$$Gap \text{ Exists if } T2 - T1 > 0 \quad Gap = T2 - T1 = 231.83 - 53 = 178.83 secs$$

→ TAKE OFF IS POSSIBLE

14. TAKEOFF BETWEEN D - B ARRIVAL:

$$T1 = Ti + ROTd = 0 + 53 = 48secs$$

$$T2 = H_{DB} - \frac{\delta}{Vb} = 232.36 - \frac{2}{110} \cdot \frac{3600secs}{1Hour} = 166.905 \text{ secs}$$

$$\text{Gap Exists if } T2 - T1 > 0 \quad \text{Gap} = T2 - T1 = 166.905 - 53 = 113.905 \text{ secs}$$

→ TAKE OFF IS POSSIBLE

15. TAKEOFF BETWEEN D - C ARRIVAL:

$$T1 = Ti + ROTd = 0 + 53 = 48secs$$

$$T2 = H_{DC} - \frac{\delta}{Vc} = 160.62 - \frac{2}{130} \cdot \frac{3600secs}{1Hour} = 105.235secs$$

$$\text{Gap Exists if } T2 - T1 > 0 \quad \text{Gap} = T2 - T1 = 105.235 - 53 = 52.23 \text{ secs}$$

→ TAKE OFF IS POSSIBLE

16. TAKEOFF BETWEEN D - D ARRIVAL:

$$T1 = Ti + ROTd = 0 + 53 = 48secs$$

$$T2 = H_{DD} - \frac{\delta}{Vd} = 96 - \frac{2}{150} \cdot \frac{3600secs}{1Hour} = 48 \text{ secs}$$

$$\text{Gap Exists if } T2 - T1 > 0 \quad \text{Gap} = T2 - T1 = 48 - 53 = -3 \text{ secs}$$

→ NO TAKE OFF IS POSSIBLE

After the results obtained, we could say that every time a smaller aircraft is following a larger arrival there is enough gap for takeoffs to take place. The total impact this will have to the airfield capacity would depend on the number of shifts between larger & smaller arrivals within an hour but it could definitely result in a major increase in the overall airport capacity. Once again, we made some error-free departures and perfect timing for ATM & pilots assumptions for this gaps analysis. The real gaps will be slightly different as they would take into account taxiways times, takeoff queues & air traffic controller workload. However, it is a really interesting field of study looking forward to increase capacity.

➤ **Gaps Optimization for 1 Runway & 2 Aircraft Types:**

For the first Scenario, we obtained the following results that we would need to study if the gap distribution could give us a better result for the airfield capacity:

Average Headway Mixed	117,91 secs
Average Headway Cycle	88,87 secs
Cycles per hour	4,05
Airfield Capacity for the grouping method	40,5

Table 20 Gaps Optimization Basic Scenario

The cases where we could not perform a takeoff according to the first results of the gap section were:

○ **TAKEOFF BETWEEN SMALL-SMALL ARRIVAL:**

Minimum time needed to perform a takeoff $T = 21$ secs (from previous section).

Number of possible gaps per cycle: 3 (Platoon of 4 small planes).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{88,87 + 21} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 4,05 \cdot 3 = 44.16 \text{ Operations per hour}$$

As the overall capacity increases, it would be a reasonable decision to apply a delay for the upcoming arrival.

○ **TAKEOFF BETWEEN SMALL-LARGE ARRIVAL:**

Minimum time needed to perform a takeoff $T = 25$ secs (from previous section).

Number of possible gaps per cycle: 1 (Only 1 shift of platoons within a cycle).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{88,87 + 25} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 4,05 \cdot 1 = 35.61 \text{ Operations per hour}$$

As the overall capacity is lower than the previous one, it would not be a reasonable decision to apply a delay for the upcoming arrival.

○ **TAKEOFF BETWEEN LARGE-LARGE ARRIVAL:**

Minimum time needed to perform a takeoff $T = 10$ secs (from previous section).

Number of possible gaps per cycle: 5 (5 possible gaps within a cycle 6 large planes/cycle).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{88,87 + 10} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 4,05 \cdot 5 = 56,29 \text{ Operations per hour}$$

As the overall capacity increases, it would be a reasonable decision to apply a delay for the upcoming arrival.

➤ GAPS optimization for 1 Runway & 4 Aircraft Types:

Average Headway Mixed	119,85 secs
Average Headway Cycle	93,51 secs
Cycles per hour	3,85 cycle
Airfield Capacity for the grouping method	38,5 operations per hour

Table 21 Gaps Optimization 2nd Scenario

1. TAKEOFF BETWEEN A - A ARRIVAL:

Minimum time needed to perform a takeoff $T = 20$ secs (from previous section).

Number of possible gaps per cycle: 1 (Only 1 possible gap between A-A arrivals).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{93,51 + 20} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 3,85 \cdot 1 = 35.56 \text{ Operations per hour}$$

As the overall capacity is lower than the previous one, it would not be a reasonable decision to apply a delay for the upcoming arrival.

2. TAKEOFF BETWEEN A – B ARRIVAL:

Minimum time needed to perform a takeoff $T = 23.56$ secs (from previous section).

Number of possible gaps per cycle: 1 (Only 1 shift of platoons within a cycle).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{93,51 + 23.56} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 3,85 \cdot 1 = 34.6 \text{ Operations per hour}$$

As the overall capacity is lower than the previous one, it would not be a reasonable decision to apply a delay for the upcoming arrival.

3. TAKEOFF BETWEEN B - B ARRIVAL:

Minimum time needed to perform a takeoff $T = 26.63$ secs (from previous section).

Number of possible gaps per cycle: 3 (3 possible gaps for B-B within a cycle).

$$\frac{1}{h_{cycle} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{CYCLE}$$

$$\frac{1}{93,51 + 26.63} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 3,85 \cdot 3 = 41.51 \text{ Operations per hour}$$

As the overall capacity increases, it would be reasonable to apply a delay for the upcoming arrival.

4. TAKEOFF BETWEEN B - C ARRIVAL:

Minimum time needed to perform a takeoff $T = 27$ secs (from previous section).

Number of possible gaps per cycle: 1 (1 possible gaps for B-C within a cycle 1 shift per cycle).

$$\frac{1}{h_{\text{cycle}} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{\text{CYCLE}}$$

$$\frac{1}{93,51 + 27} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 3,85 \cdot 1 = 33.723 \text{ Operations per hour}$$

As the overall capacity is lower than the previous one, it would not be a reasonable decision to apply a delay for the upcoming arrival.

5. TAKEOFF BETWEEN C - C ARRIVAL:

Minimum time needed to perform a takeoff $T = 20.31$ secs (from previous section).

Number of possible gaps per cycle: 1 (1 possible gaps for C-C within a cycle 1 shift per cycle).

$$\frac{1}{h_{\text{cycle}} + T} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + q[\text{Cycles}] \cdot N \left[\frac{\text{Operations}}{\text{Cycle}} \right] > A_{\text{CYCLE}}$$

$$\frac{1}{93,51 + 20.31} \cdot \frac{3600 \text{ secs}}{1 \text{ hour}} + 3,85 \cdot 1 = 35.479 \text{ Operations per hour}$$

As the overall capacity is lower than the previous one, it would not be a reasonable decision to apply a delay for the upcoming arrival.

➤ **Delay- Using Pollaczek-Khinchin formula**

Capacity for Mixed=30.53arrivals/hour Capacity for Cycle Method=40.5 Arrivals/hour

- **Mean Runway Service Time & Standard Deviation of Mean Service Time**

$$\mu = \sum_{i=A}^N \frac{ROT_i}{N} \text{ [Seconds/operation]}; \quad \sigma = \sqrt{\frac{\sum_{i=A}^N (ROT_i - \mu)^2}{N}}$$

$$\mu = 46.7secs \quad \sigma = \sqrt{\frac{(38-41.5)^2 + (45-41.5)^2}{2}} = 2.62 secs$$

The value of the mean runway service time has been taken from: (Vivek Kumar, 2009)

$$\text{Coefficient of Variation} \rightarrow Cb = \frac{\sigma}{\mu} = 0.056$$

Arrival Rate $\rightarrow \lambda_{mixed}=30.53$ Arrivals/Hour $\lambda_{Cycle}=40.53$ Arrivals per hour

- **Load Factor:**

$$\rho_{mixed} = \frac{\lambda_{mixed}}{\mu} = \frac{30.53 \cdot \frac{Arrivals}{Hour}}{46.7 \cdot \frac{Seconds}{Arrival} \cdot \frac{3600secs}{Hour}} = 0.396$$

$$\rho_{cycle} = \frac{\lambda_{cycle}}{\mu} = \frac{40.5 \cdot \frac{Arrivals}{Hour}}{46.7 \cdot \frac{Seconds}{Arrival} \cdot \frac{3600secs}{Hour}} = 0.467$$

- **Average Delay per Operation:**

$$W_{Mixed} = \frac{\rho(1 + Cb^2)}{2\mu(1 - \rho)} = \frac{0.352 \cdot (1 + 0.084^2)}{2 \cdot \frac{1}{46.7} \frac{secs}{operation} \cdot \frac{3600secs}{1Hour} \cdot (1 - 0.352)} = 0.007015 \frac{Hour}{Operation}$$

$$= 25.35 \frac{secs}{operation}$$

$$W_{cycle} = \frac{\rho(1 + Cb^2)}{2\mu(1 - \rho)} = \frac{0.467 \cdot (1 + 0.084^2)}{2 \cdot \frac{1}{41.5} \frac{secs}{operation} \cdot \frac{3600secs}{1Hour} \cdot (1 - 0.467)} = 0.0118 \frac{Hour}{Operation}$$

$$= 42.79 \frac{secs}{operation}$$

As we can see from the results obtained for the basic case, the average delay will be greater when we apply the grouping method. This could be considered as a disadvantage for the mixed operation because the planes will have to spend more time waiting which means more fuel costs and machine time. Although the example above shows a numerical difference of the average delay, we have developed a sensitivity analysis of the AVG Delay versus Capacity as shown below.

○ **Average Delay vs Capacity:**

Fig. 7 shows how the average delay changes as we increase the number of operations per hour that hypothetically an airport could perform. The 5 different colors are 5 possible coefficient of variation. It can be inferred that according to the Pollaczek-Khinchin formula, the average delay would increase exponentially in relation to the capacity.

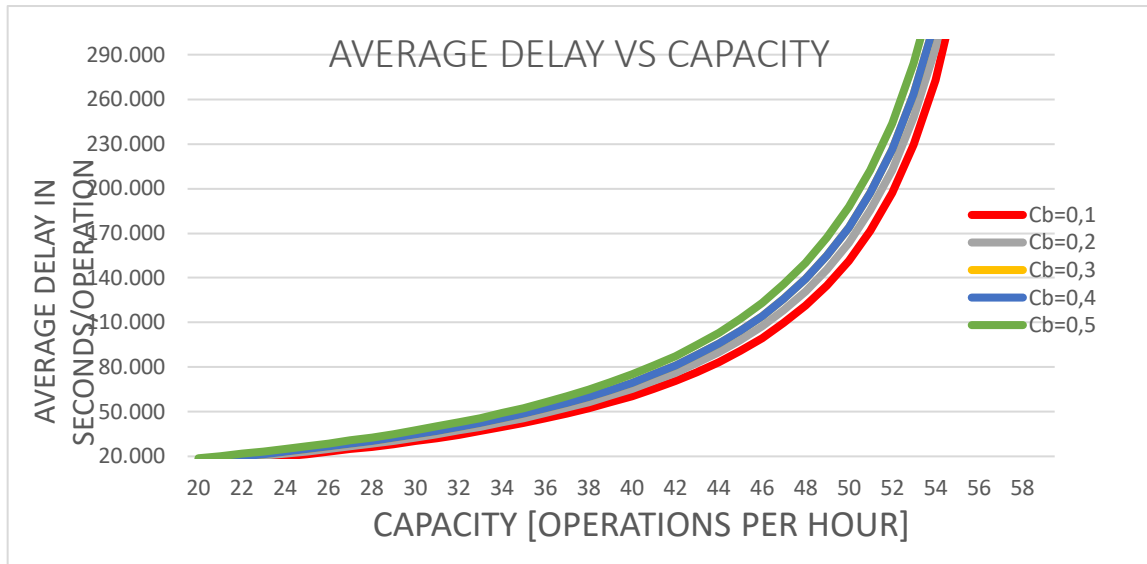
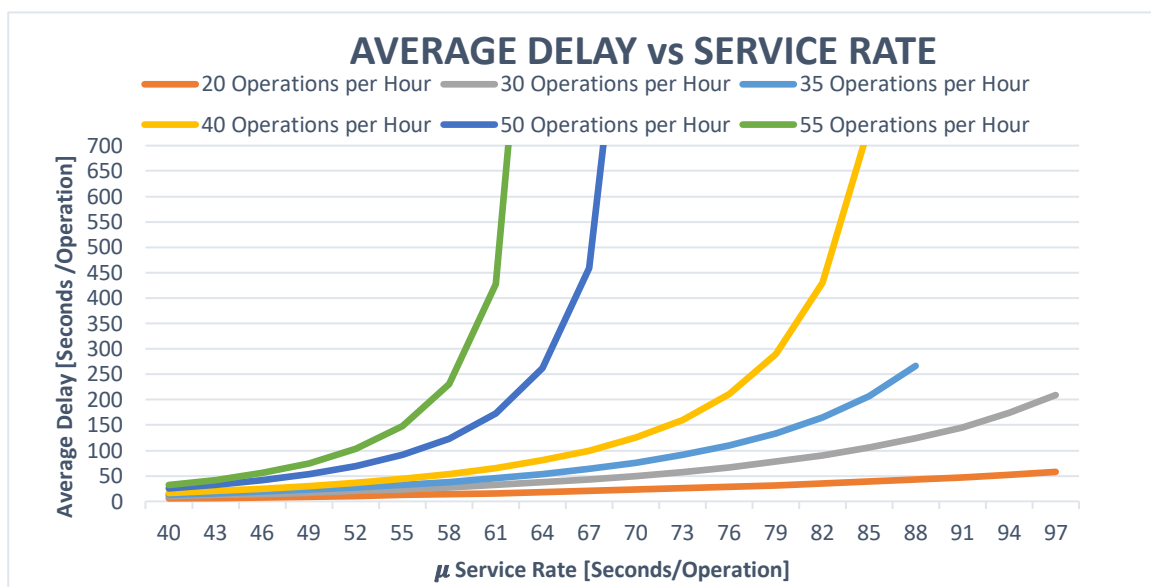


Figure 13 Average Delay versus Capacity for Given Aircraft Mix of (40% A, 60% B)



Here we can see the relation between the average delay per operation and the mean service time of the runway. Fig. 8 shows how the average delay would change for six constant capacity values at variable runway service times. It clearly shows that increasing the mean service time of the runway implies greater average delay.

➤ **Average Delay for Grouping Method:**

1st Scenario: 2 Aircrafts (A & C) & 1 Runway (Aircraft Mix: A:40% C:60%)

Small(A) Planes per cycle	4 planes
Large (C) Planes per cycle	6 planes
Planes per cycle	10 planes
Duration Small Platoon	296,7 secs
Duration Large Platoon	446,28 secs
Mean Platoon's shift duration	145,74 secs
Probability of Small Platoon	0,42
Probability of Large Platoon	0,58
Average Delay Per Cycle	441,95 secs
Average Delay per Operation	44,195secs

Table 22 Average Delay Basic Scenario Results

2nd Scenario: All Aircrafts & 1 Runway (Aircraft Mix: A:20% B:40% C:20% D:20%)

In this scenario, we will compare the average delay for a cycle of the same aircraft mix but different cycle size:

Scenario	10 Planes per Cycle	20 Planes per cycle
Duration Platoon Aircraft A	98,9 secs	296,70 secs
Duration Platoon Aircraft B	225 secs	525,00 secs
Duration Platoon Aircraft C	86,40 secs	259,20 secs
Duration Platoon Aircraft D	99,31 secs	297,93 secs
Planes type A per cycle	2 planes	2 planes
Planes type B per cycle	4 planes	4 planes
Planes type C per cycle	2 planes	2 planes
Planes type D per cycle	2 planes	2 planes
Planes per cycle	10 planes	20 planes



Mean Platoon's shift duration	125,60 secs	125,6 secs
Probability of Platoon A	0,22	0,22
Probability of Platoon B	0,35	0,35
Probability of Platoon C	0,21	0,20
Probability of Platoon D	0,22	0,23
Average Delay Per Cycle	441,95 secs	871,57 secs
Average Delay per Operation	45,47secs	44,72 secs
Airfield Capacity	39,6 operations/hour	40,51 operations/hour

Table 23 Average Delay 2nd Scenario Results

SENSITIVITY ANALYSIS

In order to obtain more information about the grouping method, the different effects it would have on five aircraft mixes have been evaluated. The five mixes analyzed are:

- 1st Scenario: A:20% B:40% C:20% D:20%
- 2nd Scenario: A:0% B:30% C:30% D:40%
- 3rd Scenario: A:10% B:40% C:50% D:0%
- 4th Scenario: A:30% B:20% C:30% D:20%
- 5th Scenario: A:10% B:20% C:30% D:40%

Firstly, the mixes have been evaluated and compared for an expected cycle size of 10 aircraft as it has been done in the previous cases. After this, an analysis of how the important factors would vary for different cycle sizes has been developed.

1. Average Headway & Capacity

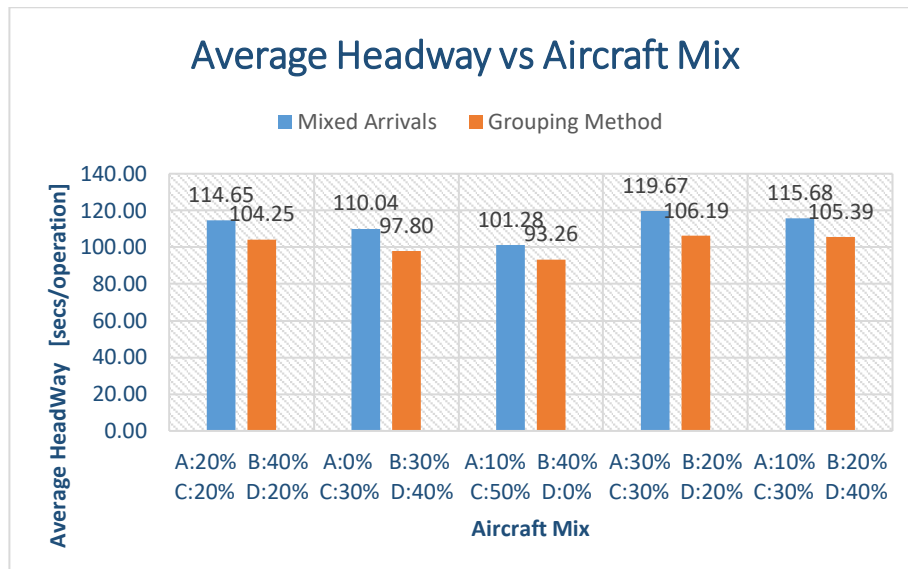


Figure 14 Avg. Headway vs Aircraft Mix

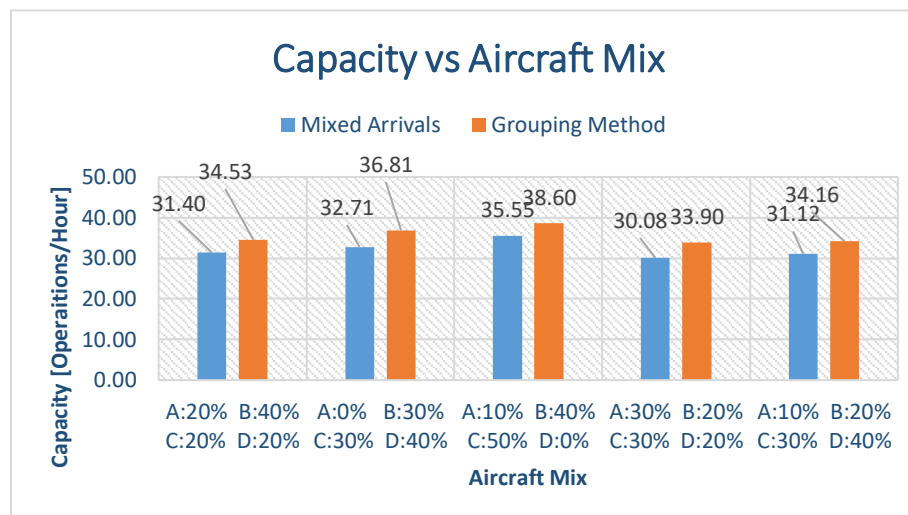


Figure 15 Capacity vs Aircraft Mix

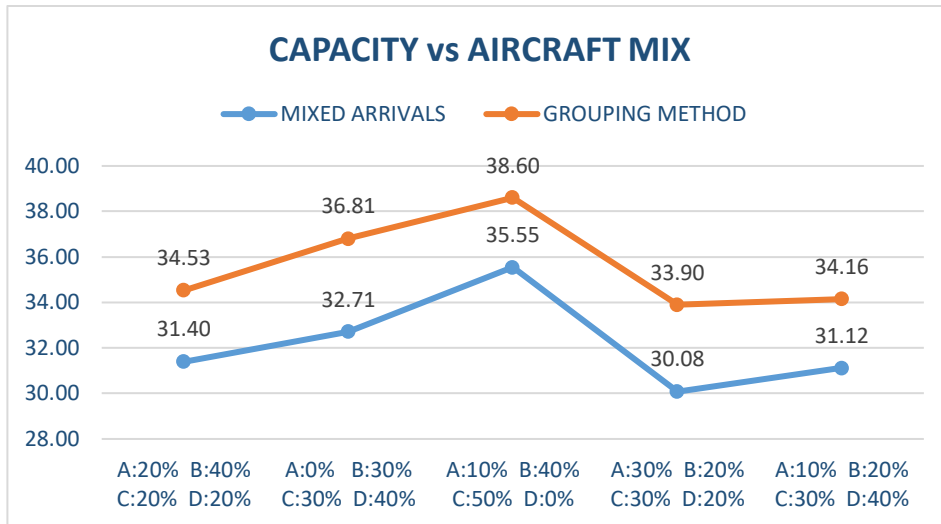


Figure 16 Capacity vs Aircraft Mix

Fig.15 & Fig.16 clearly show that in all five scenarios, the application of the grouping method would be justified as it reduces the average headway between operations which indeed, is transformed in a greater airfield capacity. Between the five scenarios, the 3rd one would obtain the best results with 38,6 operations per hour. The absence of group D in the mix could explain the results as heavy planes generate the highest wake turbulence.

2. Capacity vs Cycle Size

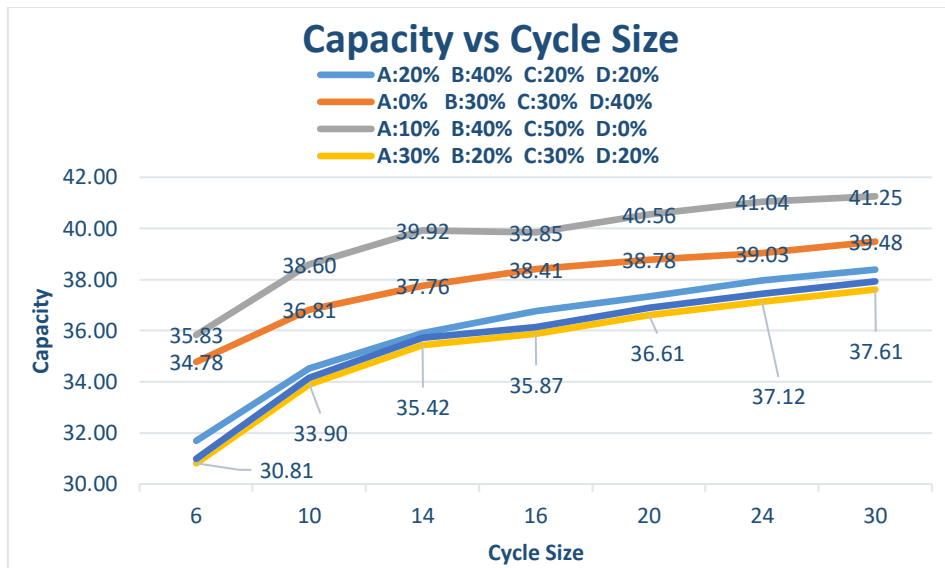


Figure 17 Capacity vs Cycle for Five Aircraft Mix

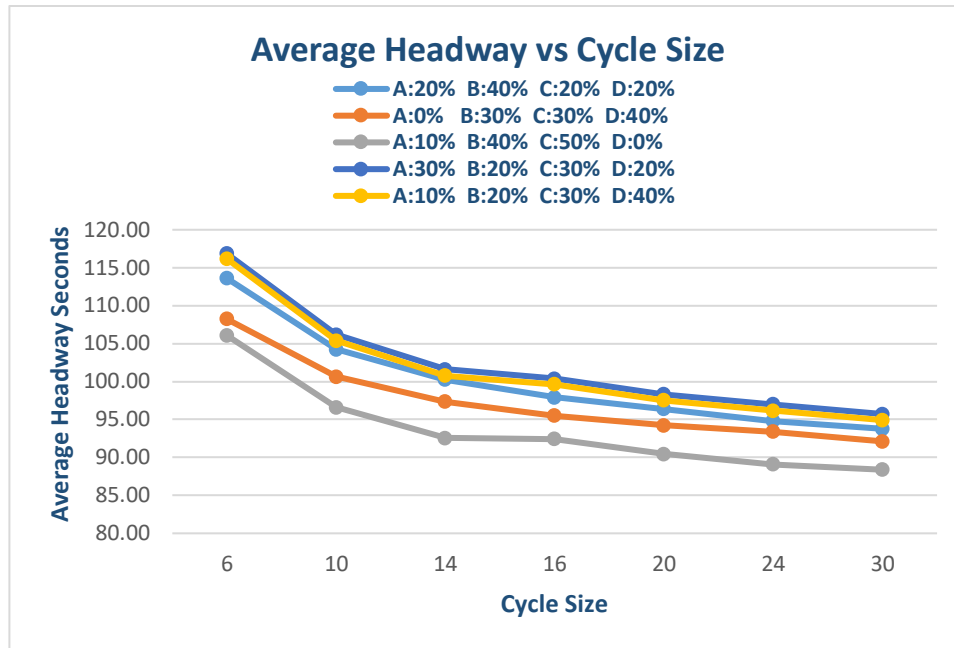


Figure 18 Avg. Headway vs Cycle Size for Five Aircraft Mix

Fig.18 & Fig 19 prove that Capacity increases alongside the cycle size. The five scenarios obtain their highest value for the biggest cycle size computed. This is because the amount of time gained in the grouping method highly relies on the total number of platoon shifts performed within an hour. Therefore, as the cycle size increases, the number of platoon shifts becomes lower resulting in a greater overall airfield capacity.

3. Average Delay vs Aircraft Mix

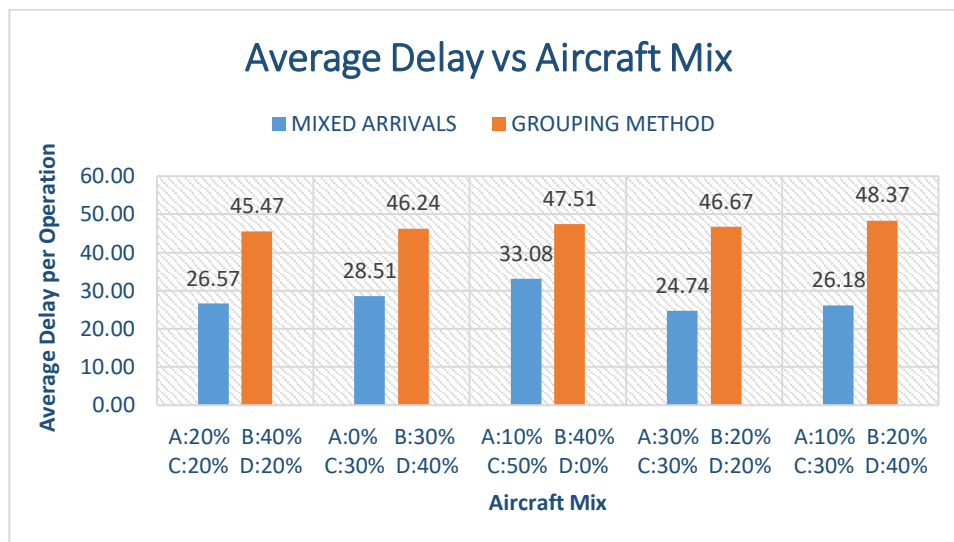


Figure 19 Avg. Delay vs Aircraft Mix

As commented in previous sections, the grouping method would not only have benefits. It produces greater average delay than mixed arrivals. In Fig.20, the difference [seconds] between both approaches is shown. Although all scenarios have similar avg. delay for the grouping

method, the 3rd Scenario would have the smallest gap (14.43 seconds) while the 5th one has the largest one (22.19 seconds).

4. Delay vs Cycle Size

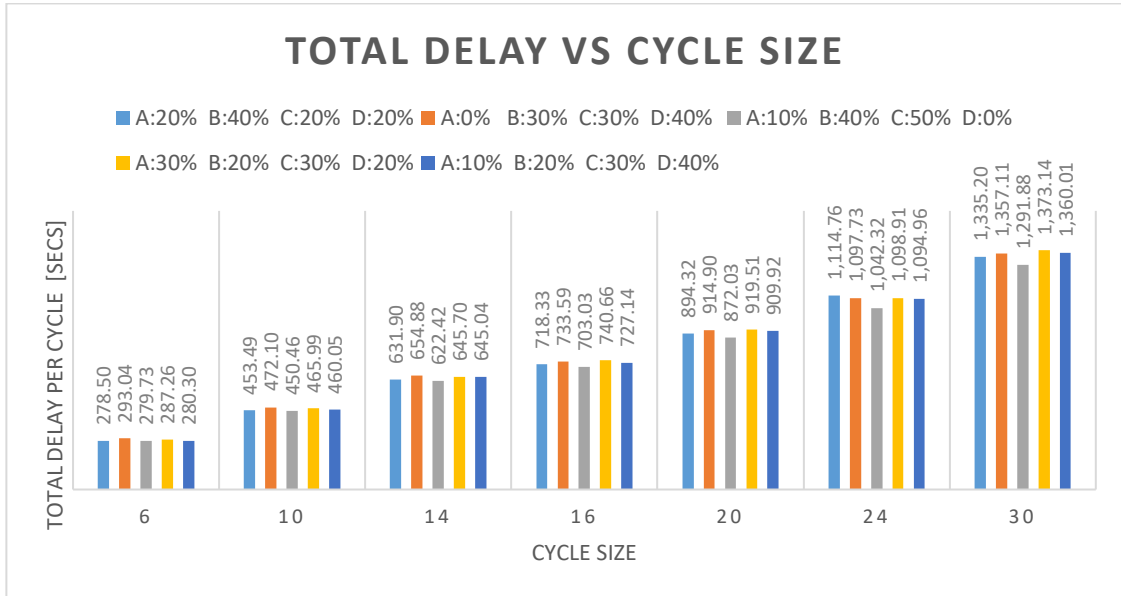


Figure 20 Total Delay vs Cycle Size

Fig. 21 shows graphically the evolution of the total delay per cycle of planes. As expected, the total delay is proportional to the amount of planes per cycle. Nevertheless, it is really interesting to analyze how the average delay varies in relation to the cycle size. The figures below illustrate the fluctuation of the delay.

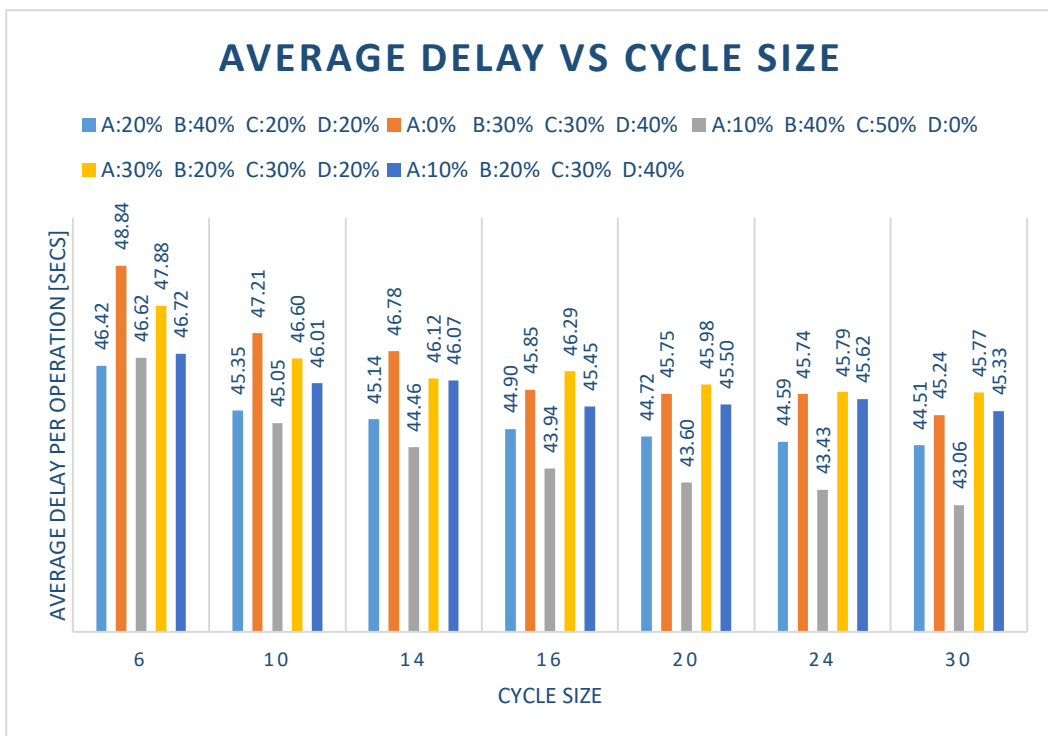


Figure 21 Avg. Delay vs Cycle Size

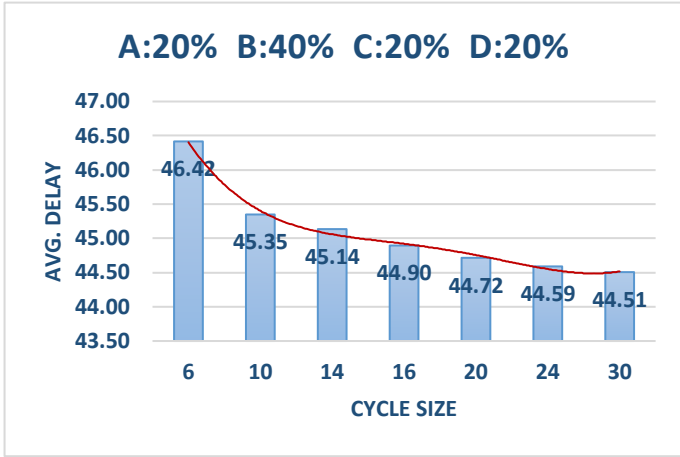


Figure 22 Avg. Delay vs Cycle Size 1st Scenario

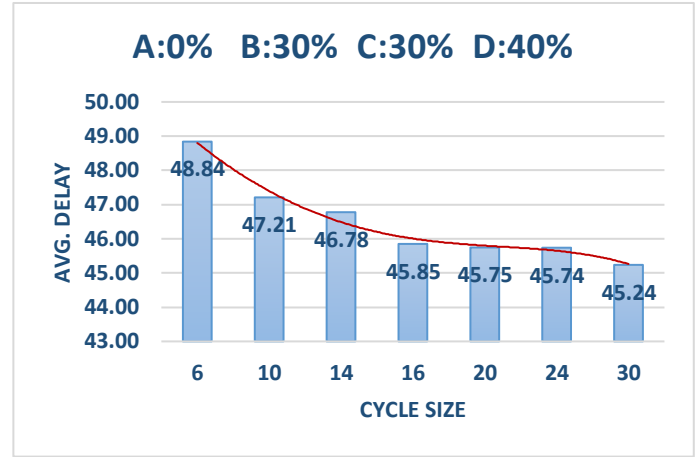


Figure 23 Avg. Delay vs Cycle Size 2nd Scenario

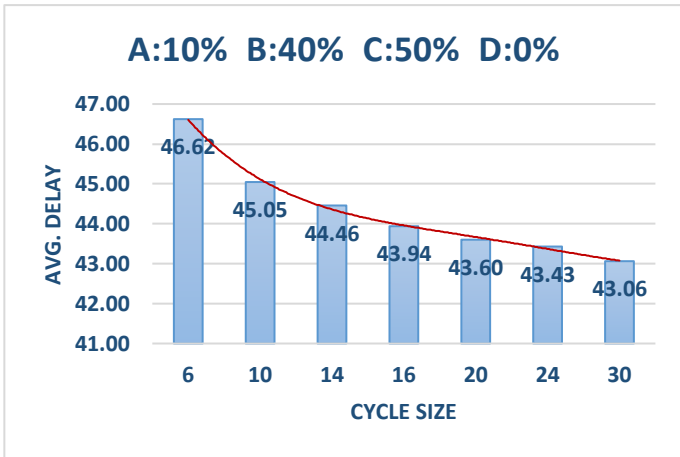


Figure 25 Avg. Delay vs Cycle Size 3rd Scenario

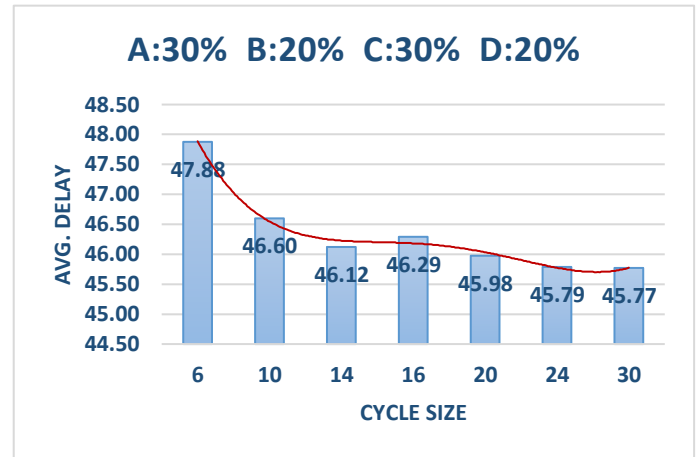


Figure 24 Avg. Delay vs Cycle Size 4th Scenario

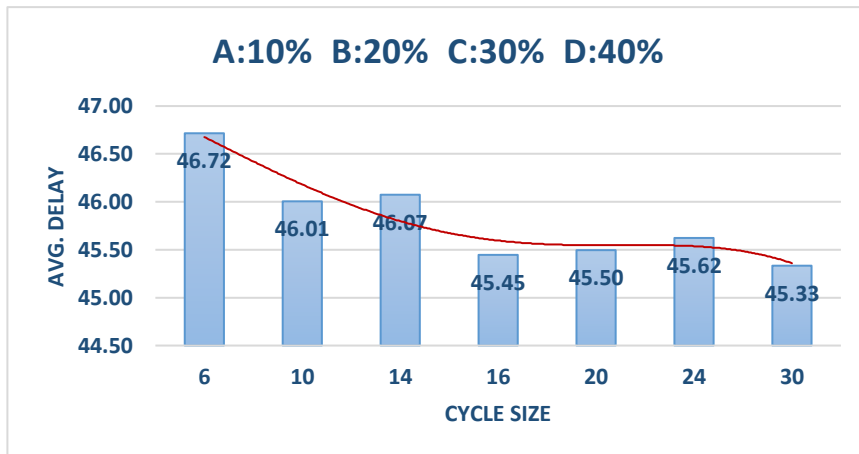


Figure 26 Avg. Delay vs Cycle Size 5th Scenario

The analysis reveals that the average delay remains almost equal for every Cycle Size apart from a small decrease. The 2nd Scenario (Fig.23) has the largest variation, 3.60 secs gap between the cycle size of 6 and 30.

SUMMARY RESULTS

1. Capacity

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	30.53 ops/hour	40.51 ops/hour
A:20% B:40% C:20% D:20%	31.40 ops/hour	34.53 ops/hour

Aircraft Mix	A:20% B:40% C:20% D:20%	A:0% B:30% C:30% D:40%	A:10% B:40% C:50% D:0%	A:30% B:20% C:30% D:20%	A:10% B:20% C:30% D:40%
Capacity	34.53	36.81	38.60	33.90	34.16

Table 24 Capacity Analysis Results

2. Average Delay

Aircraft Mix	Mixed Arrivals	Grouping Method
A:40% B:0% C:60% D:0%	25.35 secs/op	42.8 secs/op
A:20% B:40% C:20% D:20%	26.57 secs/op	45.35 secs/op

Aircraft Mix	A:20% B:40% C:20% D:20%	A:0% B:30% C:30% D:40%	A:10% B:40% C:50% D:0%	A:30% B:20% C:30% D:20%	A:10% B:20% C:30% D:40%
Avg. Delay (Mixed)	26.57	28.51	33.08	24.74	26.18
Avg. Delay (Grouping)	45.35	46.24	47.51	46.67	48.37

Table 25 Avg. Delay Analysis Results

3. Takeoffs Between Landings

➤ **2 Aircraft Types:**

Aircraft Type		Leading Aircraft	
		A	C
Trailing Aircraft	A	NO	YES
	C	NO	NO

➤ **4 Aircraft Mix – 2nd Scenario**

Aircraft Type		Leading Aircraft			
		A	B	C	D
Trailing Aircraft	A	NO	YES	YES	YES
	B	NO	NO	YES	YES
	C	NO	NO	NO	YES
	D	NO	NO	NO	NO

Table 26 Takeoffs Analysis Results

CONCLUSIONS

Air transportation is facing a big growth in terms of passenger flow, number of flights, and air traffic congestion. However, this growth sometimes cannot be responded at the same amount and rate. In this light, optimization of the airfield capacity plays a big role in order to allow current airports to squeeze their potential and respond the development of the industry. In this paper, a sensitivity analysis has been performed towards suggesting a possible solution to this growing demand, the grouping method. Therefore, after all the formulation, investigation, and results the following conclusions are made:

Summary of Analysis: Along with this paper, we have gone through different analysis related to factors that affect the airfield capacity or are strongly associated with it. Firstly, we looked at the capacity of one runway whenever is being used for landings. In this light, we developed the formulation for the grouping method and computed this capacity for two cases and aircraft mixes. Next, we studied these cases for a mixed operations runway in order to find if incorporating takeoffs between aircraft shifts could be possible. Then, we analyzed the average delay in two different approaches. We used the Pollaczek-Khinchine formula for queuing models and simulated two scenarios, and then, we developed the formulation for the grouping model in order to compare both situations. After this, we finally performed a sensitivity analysis that combines capacity, delay, and cycle size analysis for five different scenarios.

Summary of Results: According to the results obtained, it can be concluded that the grouping method implies an improvement in capacity for any aircraft mix in comparison to the FCFS. As we have seen, this gain in operations depends essentially on the aircraft mix & cycle size. There are also some other important factors, such as the approaching speed of aircrafts, or the common length approach. However, this benefit in aircraft operations results in a greater average delay that remains almost constant no matter the cycle size as the sensitivity analysis illustrate. This delay could be considered as a drawback for this technique when the airport is not congested and does not need to serve a significant number of aircrafts.

Conclusions and Recommendations about how Airports should operate: Although the study and results reflect a better capacity for the grouping method, it would not make sense for the airport to use this technique whenever it is not congested. Therefore, during periods of low demand, it would be more reasonable for the airport to operate in FCFS as the capacity will not be a problem and the average delay is better. At congested periods the grouping method could help the airport to attend the demand giving substantial progress in the number of operations per hour. The airport will have to choose between increasing the capacity or maintaining the delay

regarding their passenger flow, the number of gates, taxiways, and ATM resources available at each concrete airport.

Also, during congested periods the airport should try to incorporate as many takeoffs between landings as possible to maximize the capacity. The grouping method will enable ATM to schedule takeoffs in a more organized and easy way as the cycle sequence would be always the same. In this light, the FCFS would add more complexity and workload for the ATM as the sequence is continuously changing.

Finally, it has to be said that before incorporating the grouping method, it should be analyzed using the ATM software and instruments in order to estimate the real-life pros and cons beyond the ones in this paper.

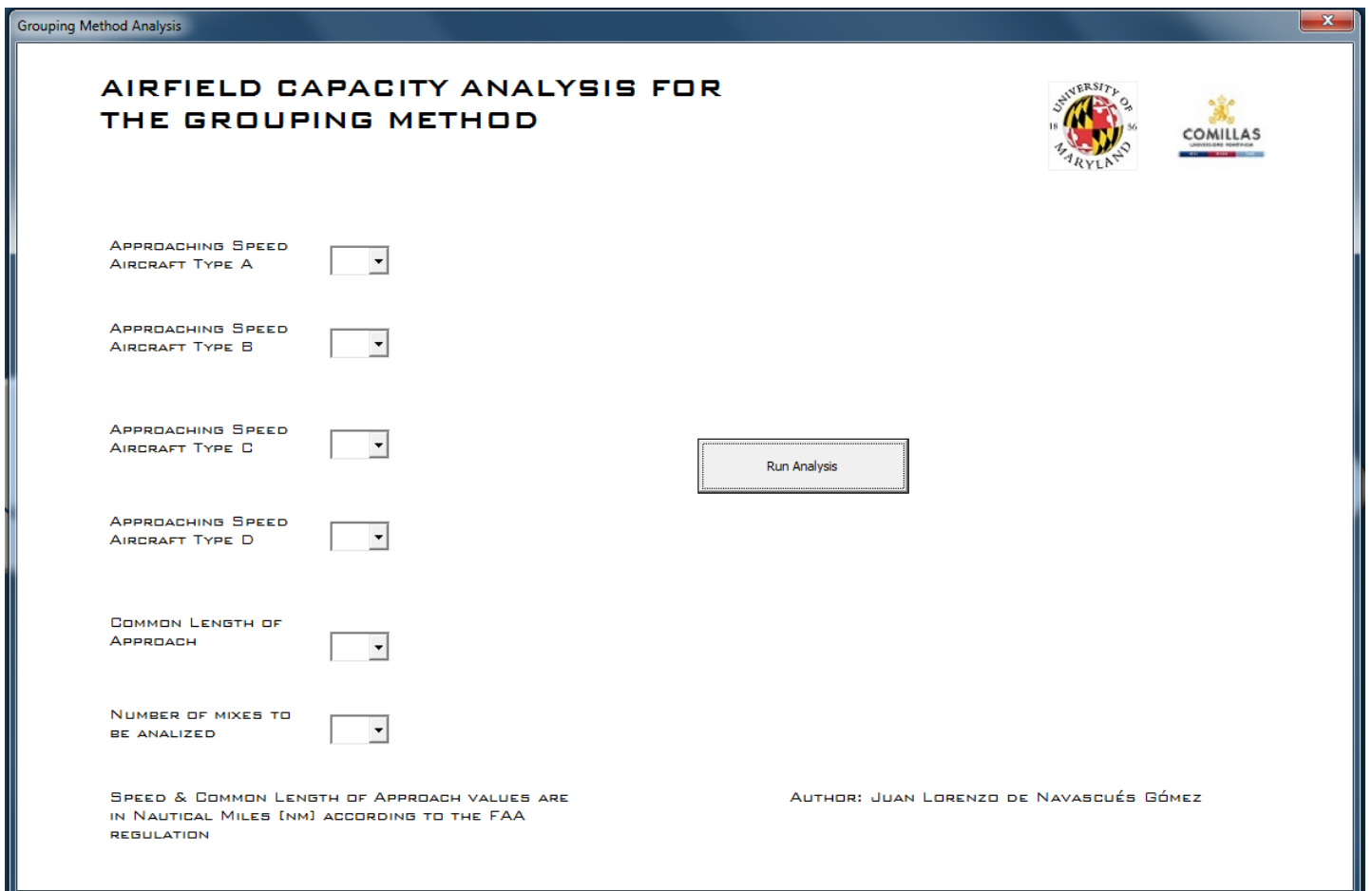
Recommendations for Further Research: In this paper, some reasonable assumptions have been made to compute the capacity and average delay. The ultimate goal of this first approach was to analyze the efficiency of the grouping method in comparison to the FCFS. In this context, it would be useful to incorporate more variables and complexity that affect this capacity in real life, such as wind speed, touchdown percentage, incomplete approaches, ATM workload or more airport layouts (more runways). Also, it could be interesting to develop software available to organize the upcoming arrivals and automatically switch between FCFS and Grouping according to the needs at the time. This paper could be used as a baseline study for future and deeper analysis of the grouping method as it initially justifies its efficacy.

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APPENDIX

General Analysis



The screenshot shows a software window titled "Grouping Method Analysis". The main heading is "AIRFIELD CAPACITY ANALYSIS FOR THE GROUPING METHOD". In the top right corner, there are logos for the University of Maryland and COMILLAS UNIVERSIDAD PONTIFICIA. The interface includes six dropdown menus for input parameters: "APPROACHING SPEED AIRCRAFT TYPE A", "APPROACHING SPEED AIRCRAFT TYPE B", "APPROACHING SPEED AIRCRAFT TYPE C", "APPROACHING SPEED AIRCRAFT TYPE D", "COMMON LENGTH OF APPROACH", and "NUMBER OF MIXES TO BE ANALYZED". A "Run Analysis" button is positioned to the right of the first three dropdown menus. At the bottom left, a note states: "SPEED & COMMON LENGTH OF APPROACH VALUES ARE IN NAUTICAL MILES [NM] ACCORDING TO THE FAA REGULATION". At the bottom right, the author is identified as "AUTHOR: JUAN LORENZO DE NAVASCUÉS GÓMEZ".

AIRFIELD CAPACITY ANALYSIS FOR THE GROUPING METHOD



APPROACHING SPEED
Aircraft Type A

APPROACHING SPEED
Aircraft Type B

APPROACHING SPEED
Aircraft Type C

Run Analysis

APPROACHING SPEED
Aircraft Type D

COMMON LENGTH OF
APPROACH

NUMBER OF MIXES TO
BE ANALYZED

SPEED & COMMON LENGTH OF APPROACH VALUES ARE
IN NAUTICAL MILES (NM) ACCORDING TO THE FAA
REGULATION

AUTHOR: JUAN LORENZO DE NAVASCUÉS BÓMEZ

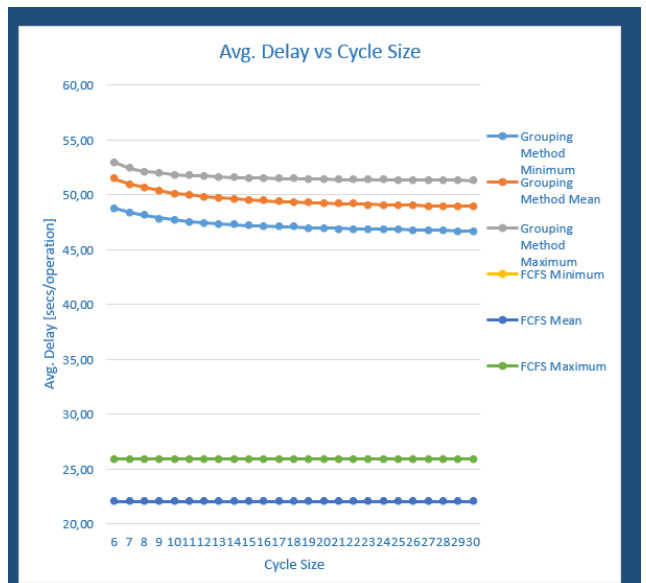
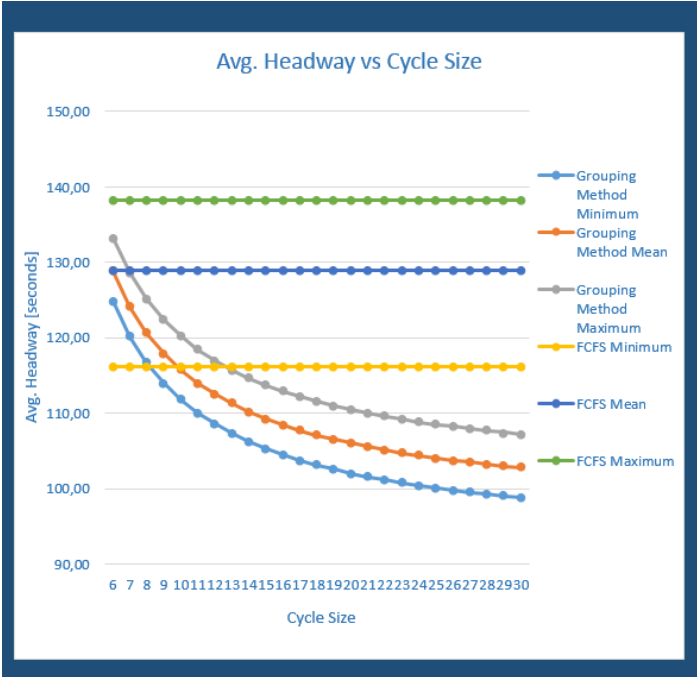
		Cycle Size																													
Aircraft Mix		6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30					
NA: 20 NB: 50 NC: 10 ND: 20	125.87	122.22	118.74	116.03	113.86	112.09	110.61	109.35	108.28	107.35	106.54	105.82	105.19	104.62	104.10	103.64	103.22	102.83	102.48	102.15	101.82	101.57	101.32	101.07	100.83						
NA: 40 NB: 30 NC: 10 ND: 20	30.04	32.40	31.91	31.20	30.76	31.22	32.55	32.92	33.25	33.53	33.79	34.02	34.22	34.41	34.58	34.74	34.88	35.01	35.13	35.24	35.35	35.44	35.53	35.62	35.70	35.78					
NA: 50 NB: 10 NC: 30 ND: 10	129.3169	124.67095	121.1865	118.47636	116.30825	114.53435	113.05609	111.80526	110.73912	109.80393	108.99089	108.2785	107.63882	107.06527	106.55177	106.08718	105.66882	105.2919	104.92569	104.60047	104.30027	104.02391	103.7642	103.5239	103.29661						
NA: 60 NB: 20 NC: 10 ND: 10	132.28975	127.6438	124.15935	121.44921	119.2811	117.5072	116.02894	114.77811	113.70597	112.77678	111.96374	111.24655	110.60888	110.03812	109.52462	109.06003	108.63767	108.25204	107.89854	107.57333	107.27313	106.99516	106.73706	106.49675	106.27246						
NA: 40 NB: 10 NC: 20 ND: 20	130.28304	125.6371	122.15264	119.4425	117.2744	115.50049	114.02223	112.7714	111.69926	110.77007	109.95703	109.23964	108.60197	108.03411	107.51791	107.05332	106.63096	106.24533	105.89183	105.56662	105.26642	104.98845	104.73035	104.49004	104.26575						
NA: 20 NB: 30 NC: 30 ND: 20	125.48323	120.83728	117.35282	114.64269	112.47458	110.70068	109.22242	107.97159	106.89945	105.97026	105.15722	104.43983	103.80215	103.2316	102.7181	102.25351	101.83115	101.44551	101.09202	100.7668	100.4666	100.18864	99.93053	99.69225	99.46599						
NA: 50 NB: 30 NC: 10 ND: 10	130.70151	126.05557	122.57111	119.86098	117.69287	115.91898	114.44071	113.18893	112.11774	111.18855	110.37551	109.65812	109.02044	108.44989	107.93639	107.47179	107.04943	106.6638	106.31031	105.98509	105.68489	105.40693	105.14882	104.90851	104.68423						
NA: 40 NB: 40 NC: 10 ND: 10	129.11328	124.46733	120.98288	118.27274	116.10463	114.33073	112.85247	111.60164	110.5295	109.60031	108.78727	108.06988	107.4322	106.86165	106.34815	105.88356	105.46612	105.07557	104.72207	104.39685	104.09665	103.81869	103.56058	103.32028	103.09599						
NA: 40 NB: 20 NC: 10 ND: 20	130.97355	126.3294	122.84496	119.13481	117.9667	116.1928	114.71454	113.46371	112.39157	111.46238	110.64894	109.93195	109.29427	108.72372	108.21022	107.74563	107.32327	106.93764	106.58414	106.25892	105.95872	105.68076	105.42285	105.18235	104.95806						
NA: 60 NB: 10 NC: 20 ND: 10	131.59744	126.9515	123.46704	120.7569	118.5888	116.81489	115.33664	114.0858	112.91466	111.84347	110.81466	110.27143	109.71585	109.24581	108.83231	108.46272	108.13652	107.84936	107.59973	107.38212	107.19202	107.02832	106.88802	106.76045	106.64475						
NA: 20 NB: 20 NC: 40 ND: 20	124.79902	120.14497	116.66052	113.95038	111.78227	110.00837	108.53011	107.27928	106.20714	105.27795	104.46491	103.74752	103.10985	102.53929	102.02579	101.56112	101.13884	100.75321	100.39971	100.0745	100.15553	99.85426	99.58225	99.32978	99.09781						
NA: 30 NB: 20 NC: 40 ND: 10	125.44812	120.80217	117.31772	114.60758	112.43947	110.66557	109.18731	107.93648	106.86434	105.93515	105.12211	104.40472	103.76703	103.19649	102.68299	102.2184	101.79604	101.40141	101.05691	100.7317	100.4315	100.15359	99.89542	99.65119	99.42332						
NA: 30 NB: 60 NC: 10 ND: 10	125.93681	121.29086	117.80641	115.09627	112.92816	111.15426	109.676	107.35303	106.42384	105.6108	104.89841	104.25573	103.68518	103.17168	102.70709	102.28473	101.8991	101.5456	101.22038	100.92018	100.64222	100.38411	100.14381	99.91951							
NA: 20 NB: 20 NC: 20 ND: 50	128.96864	124.32269	120.83824	118.1281	115.95999	114.18609	112.70783	111.457	110.38486	109.45567	108.64263	107.92524	107.28756	106.71001	106.20631	105.73892	105.31656	104.93903	104.57743	104.25221	103.95201	103.67405	103.41594	103.17564	102.95135						
NA: 20 NB: 30 NC: 20 ND: 20	127.10657	122.46062	118.97617	116.26603	114.09792	112.32402	110.84576	109.59493	108.52279	107.5936	106.78056	106.06317	105.4255	104.85494	104.34144	103.87685	103.45449	103.06886	102.71536	102.39015	102.08995	101.81198	101.55388	101.31357	101.08928						
NA: 40 NB: 20 NC: 10 ND: 20	131.63255	126.9866	123.50215	120.79201	118.6239	116.85	115.37174	114.12091	113.04877	112.11958	111.30654	110.58915	109.95147	109.38929	108.86742	108.40283	107.98047	107.59484	107.24134	106.91612	106.61592	106.33796	106.07985	105.83955	105.61526						
NA: 20 NB: 30 NC: 10 ND: 40	128.72991	124.08397	120.59951	117.88937	115.72127	113.94736	112.46911	111.21827	110.14613	109.21694	108.4039	107.68652	107.04884	106.47828	105.96478	105.50019	105.07783	104.69212	104.3387	104.01349	103.7129	103.43533	103.17722	102.93691	102.71262						
NA: 40 NB: 20 NC: 20 ND: 20	129.352	124.70606	121.2216	118.51147	116.34336	114.56945	113.0912	111.84037	110.76823	109.83904	109.026	108.30681	107.67093	107.10038	106.58688	106.12228	105.69992	105.31429	104.96808	104.63558	104.33538	104.05742	103.79991	103.559	103.33472						
NA: 50 NB: 40 NC: 10 ND: 10	130.00921	125.36326	121.87878	119.16867	117.00056	115.22666	113.7484	112.49757	111.42523	110.64832	109.96824	109.43813	108.96181	108.52813	108.12748	107.74948	107.38513	107.03519	106.69848	106.37326	106.05804	105.75282	105.45766	105.1725	104.89732						
NA: 20 NB: 50 NC: 10 ND: 20	126.86784	122.2219	118.73744	116.02731	113.8592	112.08529	110.60704	109.35621	108.28406	107.35488	106.54184	105.82445	105.19877	104.61621	104.10271	103.63812	103.21576	102.83013	102.47663	102.15422	101.87226	101.61512	101.37326	101.14515	100.92055						
NA: 40 NB: 50 NC: 20 ND: 10	125.2445	120.59856	117.1141	114.40396	112.23586	110.46195	108.98369	107.73286	106.66072	105.73153	104.91849	104.20111	103.56343	102.99287	102.47937	102.01478	101.59242	101.20679	100.85329	100.52808	100.22778	99.949914	99.691806	99.451499	99.227212						
NA: 30 NB: 30 NC: 10 ND: 20	129.38711	124.74117	121.25671	118.54658	116.37847	114.60456	113.12631	111.84538	110.80333	109.87415	109.06111	108.34772	107.70004	107.13544	106.62198	106.15739	105.73503	105.3494	104.99959	104.67069	104.37049	104.08253	103.83442	103.59411	103.36982						
NA: 40 NB: 30 NC: 20 ND: 10	126.42097	121.77503	118.29057	115.58043	113.41233	111.63842	110.16017	108.90933	107.83719	106.908	106.09496	105.37758	104.75999	104.23994	103.81954	103.40225	103.00015	102.61829	102.25162	101.90445	101.57268	101.26237	100.97129	100.70038							
NA: 60 NB: 10 NC: 10 ND: 20	132.20278	128.57484	125.09038	122.38025	120.21214	118.43823	116.95998	115.70915	114.63701	113.70782	112.89478	112.17729	111.53971	110.99916	110.55666	109.99106	109.56877	109.18007	108.82598	108.50436	108.20416	107.9262	107.66809	107.42778	107.20035						
NA: 10 NB: 20 NC: 20 ND: 50	127.3804	122.73446	119.25	116.53987	114.37176	112.59785	111.1196	109.86877	108.79663	107.86744	107.0544	106.33701	105.69933	105.12877	104.61528	104.15068	103.72832	103.34269	102.98919	102.66398	102.36378	102.08582	101.82771	101.5874	101.36311						

		Capacity																													
Aircraft Mix		6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	FCFS				
NA: 20 NB: 50 NC: 10 ND: 20	28.38	29.45	30.32	31.03	31.62	32.12	32.55	32.92	33.25	33.53	33.79	34.02	34.22	34.41	34.58	34.74	34.88	35.01	35.13	35.24	35.35	35.44	35.53	35.62	35.70	35.78					
NA: 40 NB: 30 NC: 10 ND: 20	27.68	28.71	29.53	30.20	30.76	31.22	31.66	31.99	32.25	32.57	32.81	33.03	33.22	33.40	33.56	33.70	33.84	33.96	34.07	34.18	34.28	34.37	34.45	34.53	34.61	34.67					
NA: 50 NB: 10 NC: 30 ND: 10	27.83859	28.87612	29.70628	30.38508	30.95231	31.431619	31.8426	32.198842	32.510598	32.785711	33.030283	33.249132	33.446113	33.624349	33.786393	33.934358	34.069997	34.194793	34.309994	34.41667	34.515729	34.607798	34.694045	34.77458	34.850089	34.921362					
NA: 60 NB: 20 NC: 10 ND: 10	27.21299	28.203484	28.99498	29.64202	30.18087	30.66641	31.102741	31.364865	31.606006	31.821444	32.012666	32.180611	32.347176	32.511935	32.669211	32.820944	32.967777	33.110044	33.248211	33.382611	33.513611	33.641511	33.766711	33.889611	34.010611	34.129411					
NA: 40 NB: 10 NC: 20 ND: 20	27.632146	28.659598	29.471324	30.140205	30.697238	31.166699	31.572789	31.922938	32.229398	32.499753	32.740061	32.955069	33.146571	33.323641	33.487793	33.628103	33.761302	33.888343	33.996957	34.10169	34.198841										

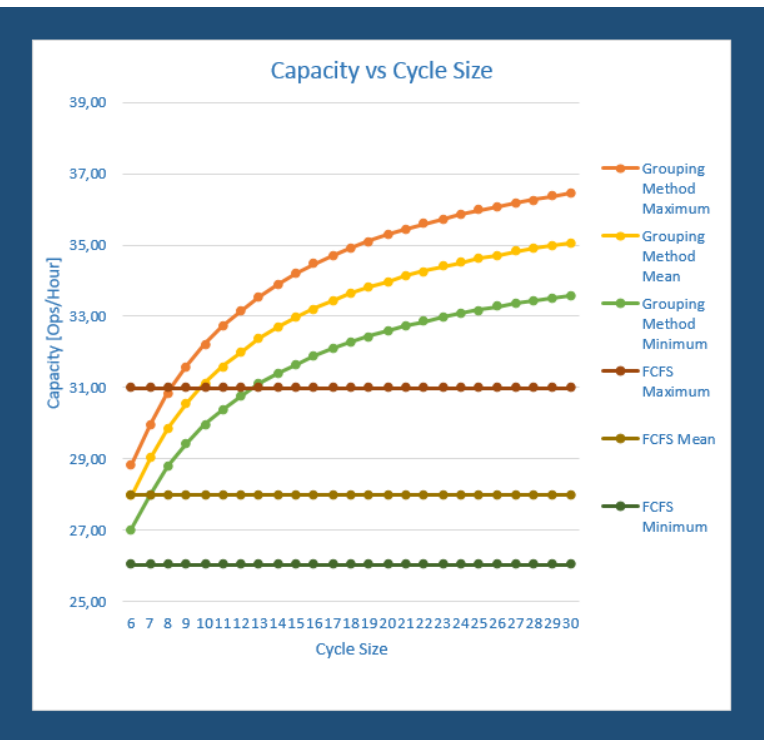
Analysis in Airfield Capacity and Delay



Average Delay Aircraft Mix	Cycle Size	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	FCFS	
NA: 40 NB: 30 NC: 10 ND: 20	50.29	49.78	49.40	49.11	48.88	48.70	48.55	48.42	48.31	48.22	48.13	48.06	48.00	47.94	47.89	47.85	47.80	47.77	47.73	47.70	47.67	47.65	47.62	47.60	47.58	23.14	
NA: 40 NB: 30 NC: 10 ND: 20	52.51	51.99	51.60	51.31	51.08	50.89	50.73	50.60	50.49	50.40	50.32	50.24	50.18	50.12	50.07	50.03	49.99	49.95	49.91	49.88	49.85	49.82	49.80	49.78	49.76	21.32	
NA: 50 NB: 10 NC: 10 ND: 10	51.575778	51.152351	50.846758	50.616821	50.438104	50.29554	50.179373	50.083026	50.001913	49.932744	49.873105	49.821182	49.77559	49.73253	49.699325	49.667129	49.635818	49.605498	49.576178	49.547858	49.520538	49.494218	49.468898	49.443578	49.418258	21.478231	
NA: 40 NB: 10 NC: 10 ND: 30	52.330794	52.008138	51.784524	51.622465	51.500814	51.406869	51.332602	51.272727	51.223643	51.182822	51.148445	51.119175	51.094011	51.072188	51.053115	51.036329	51.021461	51.008217	50.996357	50.985684	50.976037	50.967282	50.959306	50.952014	50.945325	22.706125	
NA: 40 NB: 10 NC: 20 ND: 30	52.6576	52.14282	51.74663	51.475587	51.247797	51.063832	50.912263	50.785293	50.677428	50.584688	50.50412	50.433491	50.371079	50.315536	50.265793	50.220992	50.180433	50.143545	50.109852	50.078958	50.050529	50.024283	49.999778	49.977407	49.956392	19.714225	
NA: 20 NB: 30 NC: 20 ND: 20	50.454289	50.042942	49.584463	49.128375	48.643447	48.130395	48.516237	48.351988	48.211231	48.089265	47.982617	47.888425	47.804759	47.729909	47.662552	47.601616	47.546924	47.498554	47.456491	47.420666	47.390301	47.365886	47.347924	47.335125	47.328125	22.489488	
NA: 50 NB: 30 NC: 10 ND: 10	52.201868	51.777213	51.471322	51.241355	51.063226	50.921166	50.805548	50.709716	50.629196	50.559424	50.49998	50.449484	50.398429	50.346201	50.293381	50.239401	50.184625	50.129489	50.073518	50.016378	49.958515	49.900451	49.842586	49.784321	49.725156	23.159412	
NA: 40 NB: 40 NC: 10 ND: 10	51.541493	51.065032	50.716887	50.450262	50.244221	50.076983	49.939645	49.824932	49.727737	49.64437	49.572103	49.508876	49.453106	49.403557	49.359122	49.319404	49.283378	49.250653	49.220797	49.19345	49.168312	49.145125	49.123673	49.103768	49.08525	23.829289	
NA: 40 NB: 20 NC: 10 ND: 30	52.971846	52.455643	52.076681	51.787224	51.559229	51.375183	51.223608	51.096678	50.988882	50.896228	50.815755	50.745226	50.682196	50.627474	50.577831	50.533127	50.492662	50.455865	50.422259	50.391449	50.363101	50.336922	50.312701	50.290201	50.269254	19.823884	
NA: 60 NB: 10 NC: 20 ND: 10	52.044089	51.725075	51.504067	51.343961	51.223826	51.131089	51.057807	50.998751	50.950358	50.910127	50.874337	50.842265	50.812191	50.784249	50.758923	50.7351308	50.7128293	50.691918	50.6726442	50.65416	50.636697	50.620271	50.604818	50.590318	50.576559	21.628137	
NA: 20 NB: 20 NC: 40 ND: 20	50.021743	49.427721	48.982912	48.63741	48.361319	48.135645	47.947741	47.788862	47.652768	47.538888	47.437196	47.348074	47.269089	47.197853	47.132829	47.074032	47.021057	46.974612	46.934121	46.899171	46.869266	46.844125	46.823526	46.806927	46.793927	46.784125	22.865291
NA: 30 NB: 20 NC: 40 ND: 10	50.326331	49.607376	49.139901	48.874339	48.620042	48.412946	48.241059	48.096127	47.972287	47.865256	47.771857	47.689993	47.616636	47.551479	47.492936	47.440052	47.392943	47.350627	47.313187	47.279736	47.250394	47.225099	47.199785	47.174441	47.149125	22.83523	
NA: 20 NB: 60 NC: 10 ND: 10	48.842407	48.429074	48.128935	47.904071	47.738181	47.587579	47.472797	47.377439	47.297038	47.228382	47.169111	47.11745	47.07204	47.031825	46.995974	46.963819	46.934824	46.908549	46.884632	46.862773	46.842719	46.824257	46.807206	46.791413	46.776743	25.986169	
NA: 20 NB: 10 NC: 20 ND: 50	51.45273	51.017976	50.671123	50.407309	50.200284	50.033716	49.896939	49.782704	49.68592	49.602911	49.530957	49.468008	49.412486	49.36316	49.319054	49.279389	49.243528	49.210954	49.181237	49.154019	49.129999	49.109293	49.085473	49.064763	49.046334	21.18496	
NA: 20 NB: 30 NC: 20 ND: 30	51.490946	50.89169	50.444088	50.097145	49.820396	49.594529	49.406714	49.248095	49.112362	48.994902	48.892261	48.801804	48.714484	48.64969	48.585134	48.526773	48.473759	48.425388	48.381077	48.340335	48.302748	48.267954	48.236794	48.208636	48.182667	21.406909	
NA: 50 NB: 20 NC: 10 ND: 20	52.88813	52.442114	52.118256	51.874061	51.683894	51.531929	51.407902	51.304883	51.218033	51.14388	51.079868	51.024077	50.97504	50.931614	50.8929	50.858179	50.82687	50.798498	50.772672	50.749068	50.727413	50.707477	50.689065	50.672009	50.656167	20.735731	
NA: 20 NB: 30 NC: 10 ND: 40	51.798562	51.295057	50.860242	50.555814	50.311213	50.114499	49.951852	49.815175	49.698737	49.598373	49.510985	49.434218	49.366254	49.305666	49.251319	49.202298	49.157861	49.117993	49.080388	49.04642	49.01513	48.986216	48.959458	48.911298	48.832524		
NA: 40 NB: 20 NC: 20 ND: 20	52.467347	51.923132	51.520889	51.211862	50.967225	50.768876	50.604888	50.467091	50.349706	50.248531	50.160439	50.083056	50.014549	49.953479	49.898701	49.849293	49.804504	49.763719	49.726423	49.692189	49.660555	49.631151	49.604506	49.579404	49.556014	20.793917	
NA: 50 NB: 20 NC: 10 ND: 10	52.177511	51.732114	51.409335	51.165552	50.975367	50.823212	50.698883	50.595504	50.508268	50.43372	50.369316	50.313143	50.263737	50.219958	50.180907	50.145865	50.11425	50.085389	50.059488	50.036223	50.01372	49.993349	49.974914	49.957646	49.941602	22.05468	
NA: 20 NB: 50 NC: 10 ND: 20	50.285537	49.782828	49.401761	49.113013	48.88476	48.699931	48.547293	48.419163	48.310111	48.216196	48.134485	48.062757	47.999295	47.942755	47.892066	47.846369	47.804663	47.767273	47.732821	47.70121	47.672101	47.645211	47.620995	47.597144	47.575578	23.141556	
NA: 20 NB: 50 NC: 20 ND: 10	49.045576	48.667622	48.377102	48.147018	47.964001	47.806066	47.676348	47.565821	47.470537	47.397562	47.346622	47.304662	47.270115	47.242569	47.220446	47.203182	47.190496	47.181937	47.176928	47.175105	47.176124	47.179556	47.184281	47.189981	47.196814	22.12106	
NA: 30 NB: 30 NC: 10 ND: 30	52.366095	51.805066	51.389388	51.069376	50.815591	50.609504	50.438886	50.295345	50.172935	50.067326	49.974294	49.894387	49.822708	49.758768	49.701382	49.649593	49.602621	49.559827	49.520678	49.484728	49.451601	49.420977	49.392584	49.366187	49.341582	20.547081	
NA: 40 NB: 30 NC: 20 ND: 10	51.77406	51.249224	50.864106	50.566789	50.335388	50.146418	49.990382	49.859413	49.747956	49.651797	49.568478	49.495184	49.430341	49.372572	49.320785	49.2741	49.2318	49.193298	49.158105	49.125814	49.096081	49.068614	49.043185	49.019519	48.997492	22.699054	
NA: 60 NB: 10 NC: 10 ND: 10	52.714689	52.389796	52.1648	52.001847	51.879601	51.78525	51.710701	51.650628	51.601405	51.56045	51.52604	51.496724	51.471529	51.449688	51.430066	51.413816	51.399951	51.387313	51.375861	51.365399	51.355955	51.348424	51.342862	51.338985	51.329585	51.322912	20.327898
NA: 10 NB: 20 NC: 20 ND: 50	50.790515	50.312562	49.962302	49.695192	49.485097	49.315177	49.176381	49.059822	48.960626	48.875996	48.80229	48.737739	48.680747	48.63007	48.584719	48.543901	48.506973	48.473407	48.442766	48.414685	48.388958	48.365025	48.342964	48.322486	48.303427	22.177228	





Gap for a takeoff between two consecutive landings [seconds]				
TRAILING AIRCRAFT	LEADING AIRCRAFT			
	A	B	C	D
A	-22,92	7,94	111,25	184,93
B	-26,10	-27,00	66,78	130,93
C	-30,25	-31,15	-19,07	46,47
D	-31,69	-32,59	-21,93	-1,27



3 Specific Case Analysis

3 Scenario Analysis X

	A	B	C	D
AIRCRAFT MIX 1	20	30	30	20
AIRCRAFT MIX 2	40	10	20	30
AIRCRAFT MIX 3	10	0	30	60
APPROACHING SPEED OF AIRCRAFT A	90	105	135	155
COMMON LENGTH OF APPROACH	5			

Run Analysis

AUTHOR: JUAN LORENZO DE NAVASCUÉS GÓMEZ

Average Headway	Cycle Size																														fixed Arrivals
Aircraft Mix	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30						
%A: 20 %B: 30 %C: 30 %D: 20	119,28	114,85	111,53	108,95	106,89	105,20	103,79	102,60	101,57	100,69	99,91	99,23	98,62	98,08	97,59	97,15	96,75	96,38	96,04	95,73	95,45	95,18	94,93	94,71	94,49	120,67					
%A: 40 %B: 10 %C: 20 %D: 30	129,43	119,00	115,68	113,10	111,03	109,34	107,94	106,74	105,72	104,84	104,06	103,38	102,77	102,23	101,74	101,30	100,89	100,53	100,19	99,88	99,59	99,33	99,08	98,85	98,64	131,00					
%A: 10 %B: 0 %C: 30 %D: 60	120,72845	116,30181	112,98182	110,39961	108,33385	106,64367	105,23519	104,0434	103,02187	102,13654	101,36188	100,67835	100,07077	99,527151	99,03789	98,595226	98,192804	97,825375	97,488565	97,178699	96,89267	96,627828	96,381303	96,152939	95,939239	111,8					

Capacity	Cycle Size																														FCFS
Aircraft Mix	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30						
%A: 20 %B: 30 %C: 30 %D: 20	30,18	31,34	32,28	33,04	33,68	34,22	34,69	35,09	35,44	35,75	36,03	36,28	36,50	36,70	36,89	37,06	37,21	37,35	37,48	37,61	37,72	37,82	37,92	38,01	38,10	29,83					
%A: 40 %B: 10 %C: 20 %D: 30	29,17	30,25	31,12	31,83	32,42	32,92	33,35	33,73	34,05	34,34	34,59	34,82	35,03	35,22	35,38	35,54	35,68	35,81	35,93	36,04	36,15	36,24	36,33	36,42	36,50	27,48					
%A: 10 %B: 0 %C: 30 %D: 60	29,818986	30,953947	31,863533	32,60881	33,230612	33,757277	34,209088	34,600944	34,944036	35,246934	35,516311	35,757438	35,974539	36,171034	36,349724	36,512924	36,662565	36,800268	36,927408	37,045155	37,154513	37,256348	37,35141	37,440353	37,52375	32,200358					

Average Delay	Cycle Size																														FCFS
Aircraft Mix	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30						
%A: 20 %B: 30 %C: 30 %D: 20	48,16	47,58	47,14	46,79	46,52	46,30	46,11	45,95	45,82	45,70	45,60	45,50	45,42	45,35	45,29	45,23	45,18	45,13	45,08	45,04	45,00	44,97	44,94	44,91	44,88	24,41					
%A: 40 %B: 10 %C: 20 %D: 30	49,86	49,36	48,99	48,71	48,49	48,31	48,16	48,04	47,93	47,84	47,76	47,69	47,63	47,58	47,53	47,49	47,45	47,41	47,38	47,35	47,32	47,29	47,27	47,25	47,23	21,42					
%A: 10 %B: 0 %C: 30 %D: 60	46,704755	46,991871	46,172395	46,011533	45,8895	45,794317	45,71836	45,656575	45,605495	45,562669	45,526327	45,495155	45,468167	45,444804	45,423878	45,405523	45,389168	45,374516	45,361322	45,349386	45,338543	45,328652	45,319599	45,311283	45,303622	27,735742					

